

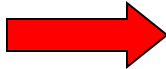
# EE 435

## Lecture 8:

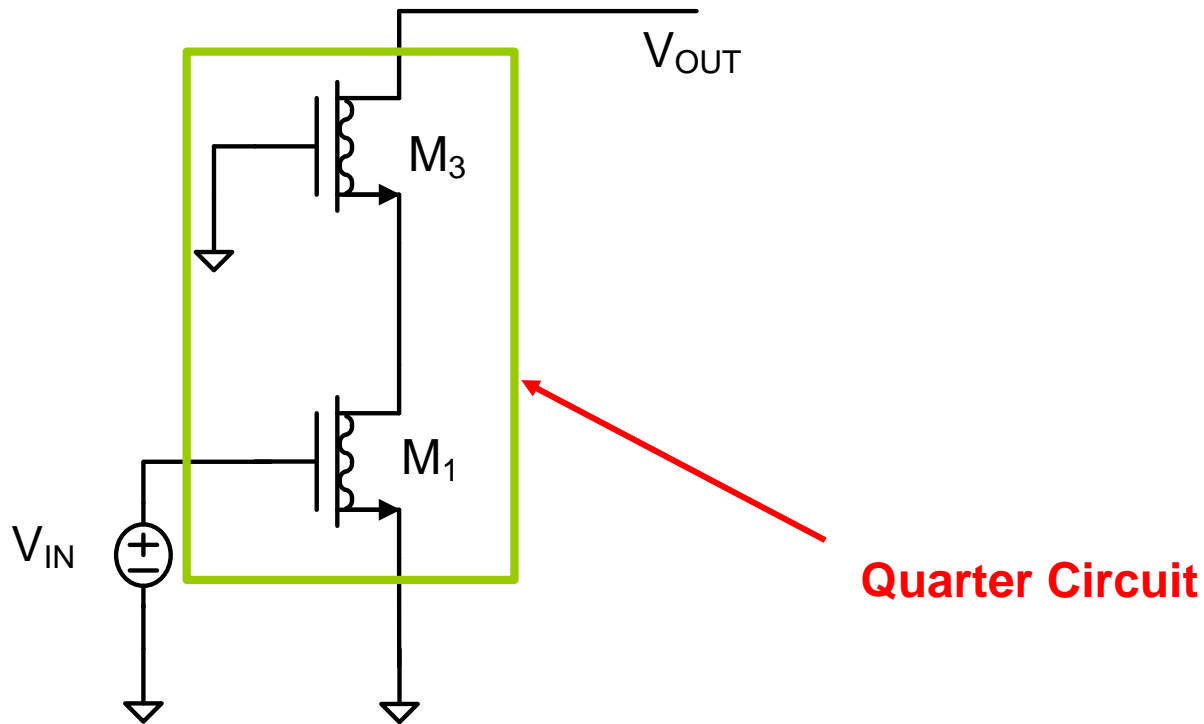
### High-Gain Single-Stage Op Amps

# Executive Summary of Last Lecture

# Basic Op Amp Design

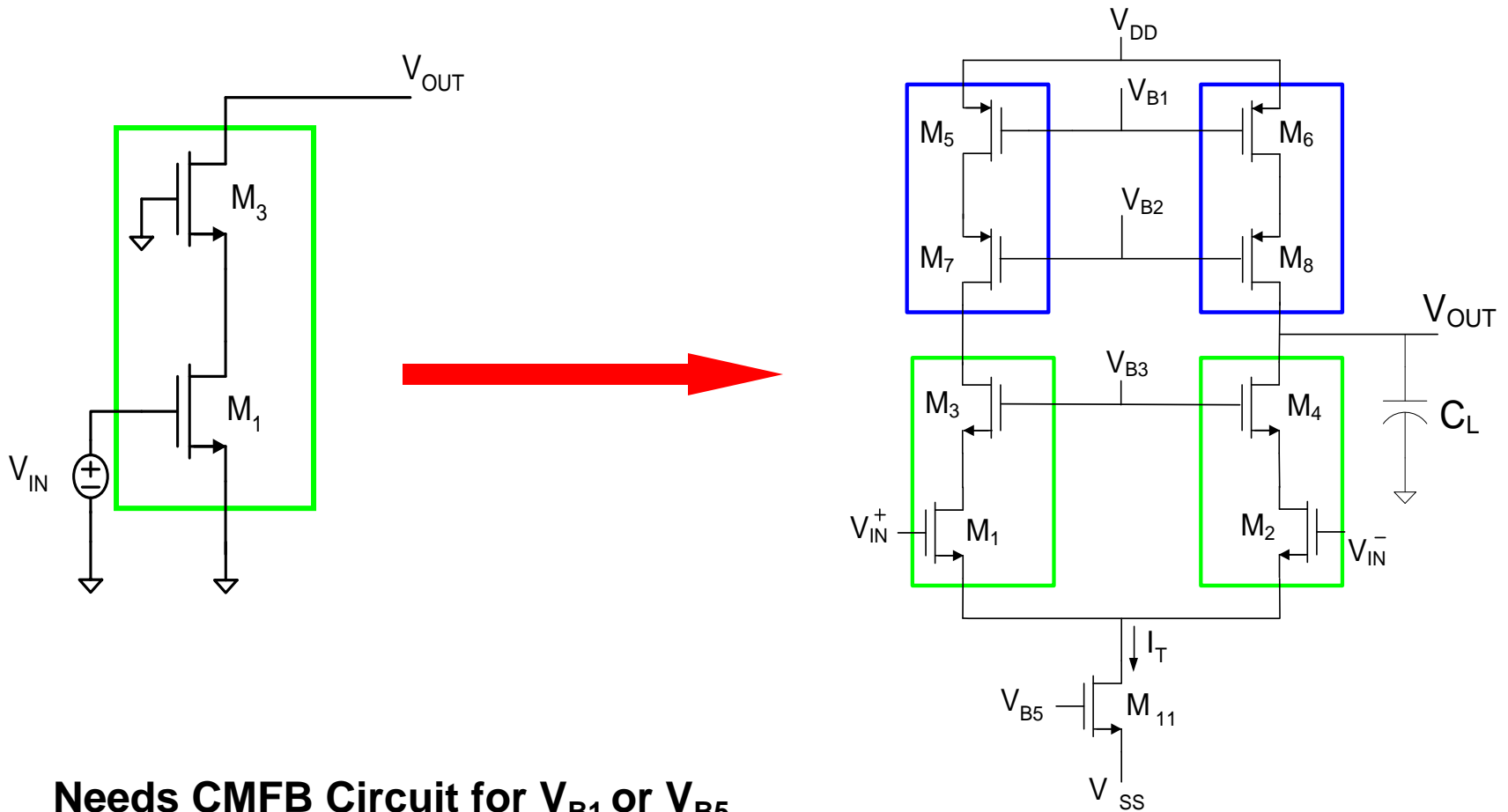
- Fundamental Amplifier Design Issues
- Single-Stage Low Gain Op Amps
-  • Single-Stage High Gain Op Amps
- Other Basic Gain Enhancement Approaches
- Two-Stage Op Amp

# High output impedance quarter-circuits



**Cascode Amplifier  
(small-signal equiv)**

# Telescopic Cascode Op Amp

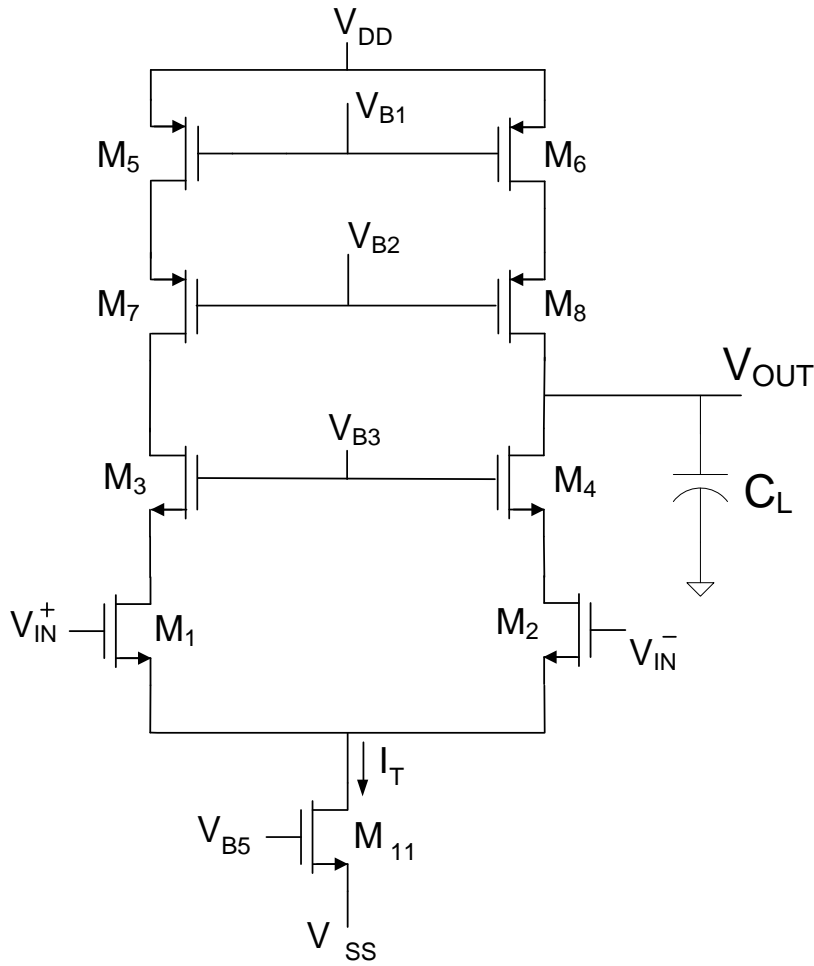


**Needs CMFB Circuit for  $V_{B1}$  or  $V_{B5}$**

**Either single-ended or differential outputs**

**Can connect counterpart as current mirror to eliminate CMFB**

# Telescopic Cascode Op Amp



(CMFB circuit not shown)

## Single-ended operation

$$A_d(s) = \frac{-\frac{g_{m1}}{2}}{sC_L + g_{o1} \frac{g_{o3}}{g_{m3}} + g_{o5} \frac{g_{o7}}{g_{m7}}}$$

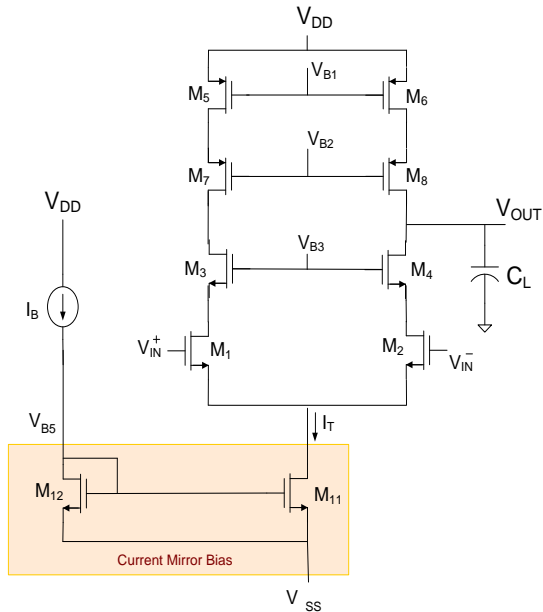
$$A_0 = \frac{-\frac{g_{m1}}{2}}{g_{o1} \frac{g_{o3}}{g_{m3}} + g_{o5} \frac{g_{o7}}{g_{m7}}}$$

$$GB = \frac{g_{m1}}{2C_L}$$

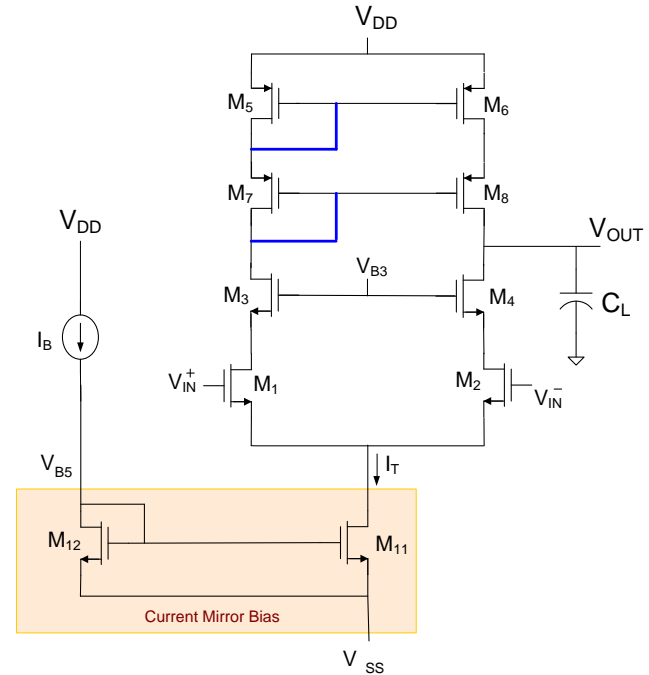
- Large improvement in  $A_0$
- No change in GB

This circuit is widely used !!

# Telescopic Cascode Op Amp

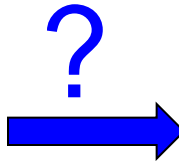


(CMFB circuit needed)



(No CMFB circuit needed)

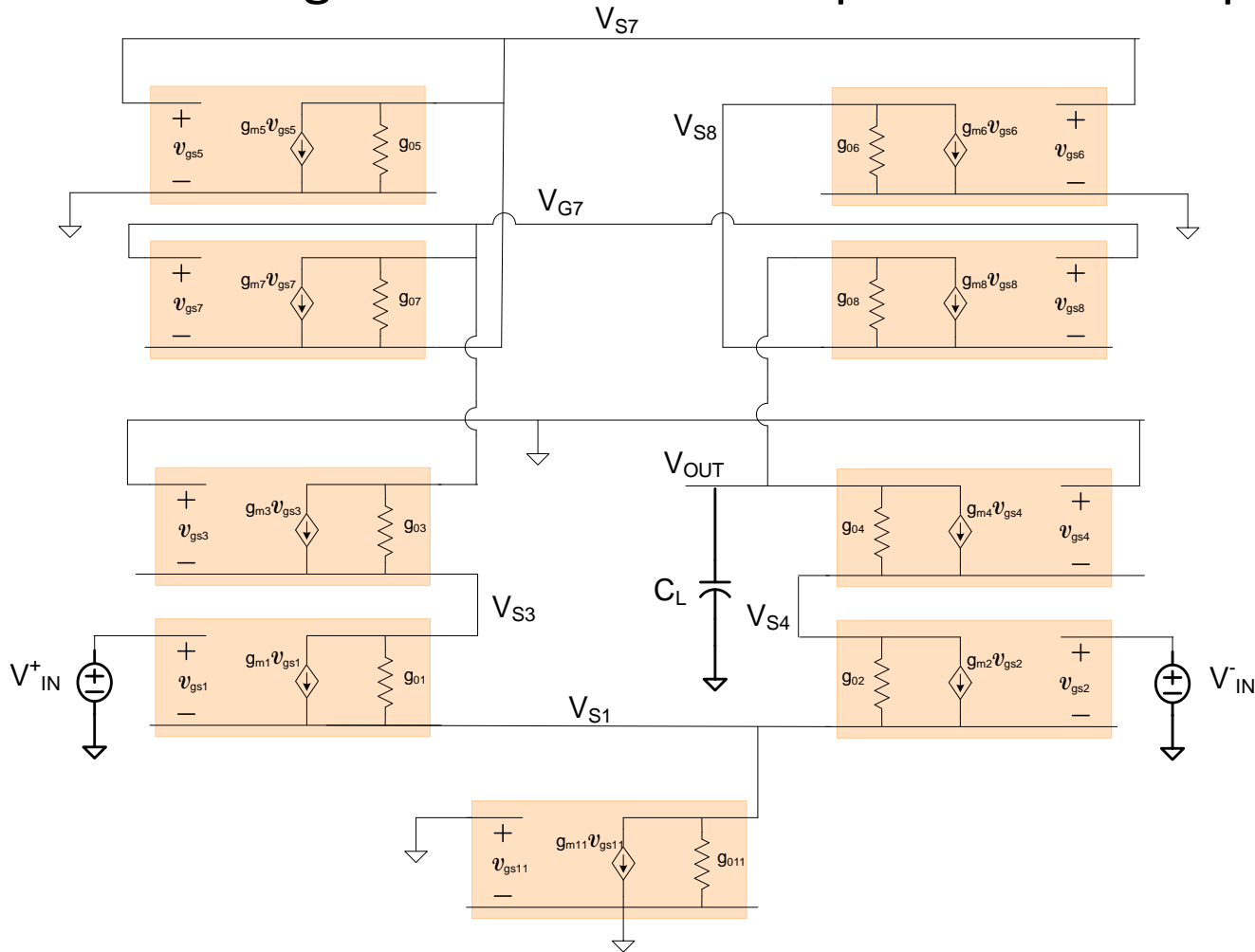
$$A_d(s) = \frac{-\frac{g_{m1}}{2}}{sC_L + g_{o1} \frac{g_{o3}}{g_{m3}} + g_{o5} \frac{g_{o7}}{g_{m7}}}$$



$$A_d(s) = \frac{-g_{m1}}{sC_L + g_{o1} \frac{g_{o3}}{g_{m3}} + g_{o5} \frac{g_{o7}}{g_{m7}}}$$

## Review from Last Lecture

# Small-Signal model of Telescopic Cascode Amplifier



A bit tedious to obtain but really straight forward



## Review from Last Lecture

# Analysis of Telescopic Cascode Amplifier

Apply KCL at 7 nodes to obtain a set of 7 independent linear equations

$$\left. \begin{aligned} V_{S1} (g_{01} + g_{02} + g_{011}) &= V_{S3} g_{01} + V_{S4} g_{02} + g_{m1} (V_{IN}^+ - V_{S1}) + g_{m2} (V_{IN}^- - V_{S1}) \\ V_{S3} (g_{01} + g_{03}) + g_{m1} (V_{IN}^+ - V_{S1}) &= g_{01} V_{S1} + g_{03} V_{G7} - g_{m3} V_{S3} \\ V_{S4} (g_{02} + g_{04}) + g_{m2} (V_{IN}^- - V_{S1}) &= g_{02} V_{S1} + g_{04} V_{OUT} - g_{m4} V_{S4} \\ V_{OUT} (sC_L + g_{04} + g_{08}) - g_{m4} V_{S4} + g_{m8} (V_{G7} - V_{S8}) &= g_{04} V_{S4} + g_{08} V_{S8} \\ V_{G7} (g_{07} + g_{03}) + g_{m7} (V_{G7} - V_{S7}) - g_{m3} V_{S3} &= g_{03} V_{S3} + g_{07} V_{S7} \\ V_{S8} (g_{06} + g_{08}) + g_{m8} V_{S7} &= g_{m8} (V_{G7} - V_{S8}) + V_{OUT} g_{08} \\ V_{S7} (g_{05} + g_{07}) + g_{m5} V_{S7} &= g_{m7} (V_{G7} - V_{S7}) + g_{07} V_{G7} \end{aligned} \right\}$$

A bit tedious to obtain but really straight forward

Time required to obtain set of equations is quite small

## Review from Last Lecture

# Individual product terms have product of 7 small-signal parameters

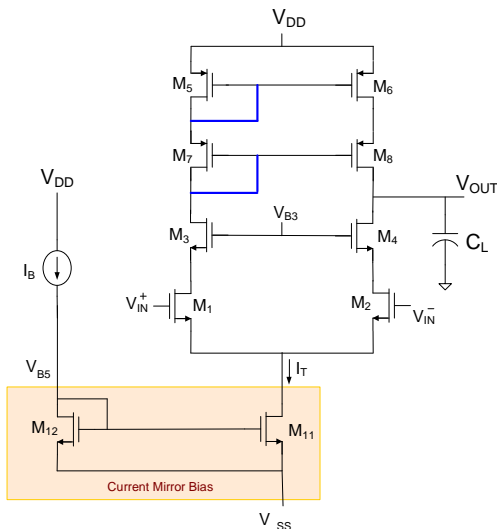
- Approximately 2000 factors in output characteristics
- Approximately 14,000 small-signal parameter appearances
- GB expression much longer

$$\frac{V_{in}p \cdot g_{08} \cdot g_{m1} \cdot g_{m2} \cdot g_{m3} \cdot g_{m4} \cdot g_{m5} \cdot g_{m7} + V_{in}p \cdot g_{06} \cdot g_{m1} \cdot g_{m2} \cdot g_{m3} \cdot g_{m4} \cdot g_{m7} \cdot g_{m8} + V_{in}p \cdot g_{08} \cdot g_{m1} \cdot g_{m2} \cdot g_{m3} \cdot g_{m4} \cdot g_{m7} \cdot g_{m8} + V_{in}p \cdot g_{m1} \cdot g_{m2} \cdot g_{m3} \cdot g_{m4} \cdot g_{m5} \cdot g_{m7} \cdot g_{m8}}{(g_{01} \cdot g_{02} \cdot g_{03} \cdot g_{04} \cdot g_{07} \cdot g_{m8}^2 + g_{01} \cdot g_{02} \cdot g_{03} \cdot g_{04} \cdot g_{m7} \cdot g_{m8}^2 + g_{01} \cdot g_{02} \cdot g_{04} \cdot g_{07} \cdot g_{m3} \cdot g_{m8}^2 + g_{02} \cdot g_{03} \cdot g_{04} \cdot g_{07} \cdot g_{m1} \cdot g_{m8}^2 + g_{01} \cdot g_{02} \cdot g_{04} \cdot g_{m3} \cdot g_{m7} \cdot g_{m8}^2 + g_{02} \cdot g_{03} \cdot g_{04} \cdot g_{m1} \cdot g_{m7} \cdot g_{m8}^2 +$$

$$CL \cdot g_{02} \cdot g_{m3} \cdot g_{m4} \cdot g_{m5} \cdot g_{m7} \cdot g_{m8} \cdot s + CL \cdot g_{03} \cdot g_{m2} \cdot g_{m4} \cdot g_{m5} \cdot g_{m7} \cdot g_{m8} \cdot s + CL \cdot g_{04} \cdot g_{m2} \cdot g_{m3} \cdot g_{m5} \cdot g_{m7} \cdot g_{m8} \cdot s + CL \cdot g_{05} \cdot g_{m2} \cdot g_{m3} \cdot g_{m4} \cdot g_{m7} \cdot g_{m8} \cdot s + CL \cdot g_{07} \cdot g_{m2} \cdot g_{m3} \cdot g_{m4} \cdot g_{m5} \cdot g_{m8} \cdot s + CL \cdot g_{08} \cdot g_{m2} \cdot g_{m3} \cdot g_{m4} \cdot g_{m5} \cdot g_{m7} \cdot s + CL \cdot g_{011} \cdot g_{m3} \cdot g_{m4} \cdot g_{m5} \cdot g_{m7} \cdot g_{m8} \cdot s + CL \cdot g_{m1} \cdot g_{m3} \cdot g_{m4} \cdot g_{m5} \cdot g_{m7} \cdot g_{m8} \cdot s + CL \cdot g_{m2} \cdot g_{m3} \cdot g_{m4} \cdot g_{m5} \cdot g_{m7} \cdot g_{m8} \cdot s)$$

## Where this started

# Telescopic Cascode Op Amp with Mirror-connected Counterpart Circuit



$$A_d(s) = \frac{-g_{m1}}{sC_L + g_{o1} \frac{g_{o3}}{g_{m3}} + g_{o5} \frac{g_{o7}}{g_{m7}}}$$

$$A_d(s) = \frac{-g_{m7}g_{m1}g_{m3}}{sC_L g_{m7}g_{m3} + g_{m7}g_{o3}g_{o1} + g_{m3}g_{o5}g_{o7}}$$

- Some assumptions were made to simplify analysis
  - $V_{ac}=0$  at “approximate axis of symmetry”
  - Matched left and right side transistors
  - Current mirror used to mirror left-side current to right side
- Difference Mode Gain has only approximately 1100 product terms
- Difference Mode Gain has approximately 7700 small-signal parameters in expression

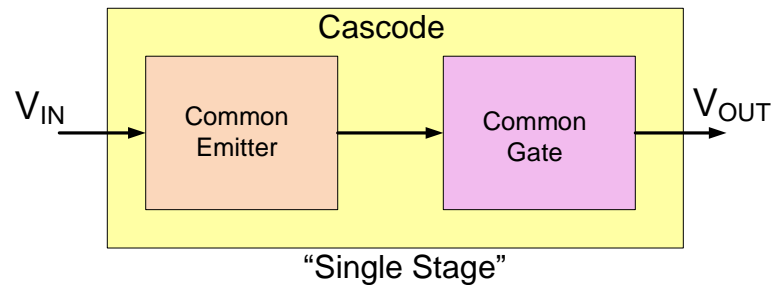
How many product terms are present in the simplified analysis?

How many small-signal parameters are in simplified expression?

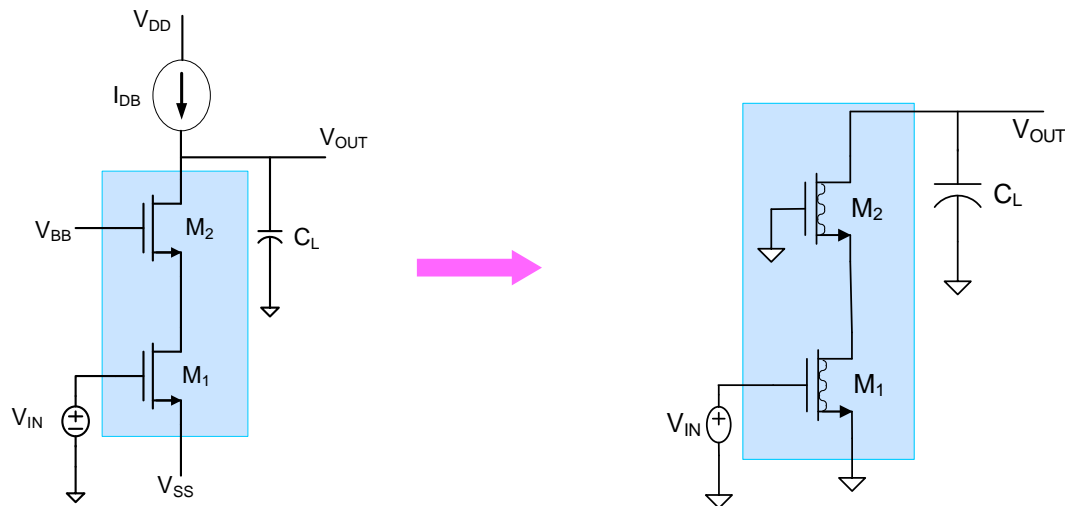
- Simplified Difference Mode Gain has 4 product terms
- Simplified Difference Mode Gain has 12 small-signal parameters in expression

# Amplifier Nomenclature

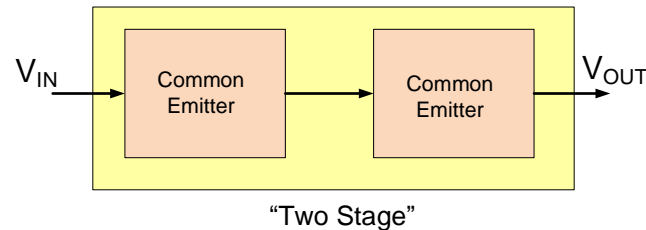
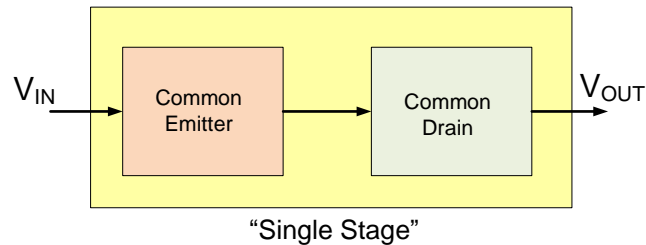
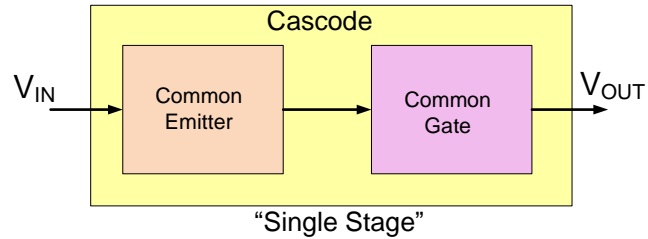
The Cascode Amplifier has been classified as a single-stage amplifier but is actually a cascade of a common-emitter stage and a common gate stage



## Cascode Amplifier

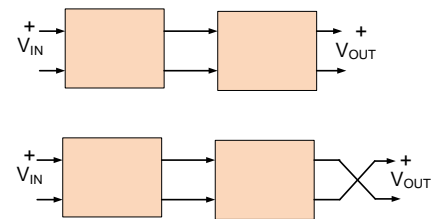


# Amplifier Nomenclature



- Single-stage amplifiers have one signal inversion

(but with differential input and differential output the polarity of signals can be identified two different ways)



- Single-stage amplifiers naturally behave approximately as first-order systems until really high frequencies

Strategy now to decrease  $G_1$  and  $G_2$  without degrading  $G_{M1}$  by very much

$$A_{VO} = \frac{-G_{M1}}{2(G_1 + G_2)}$$

$$BW = \frac{G_1 + G_2}{C_L}$$

$$GB = \frac{G_{M1}}{2C_L}$$

Are there other high output impedance circuits that can be used as quarter circuits?

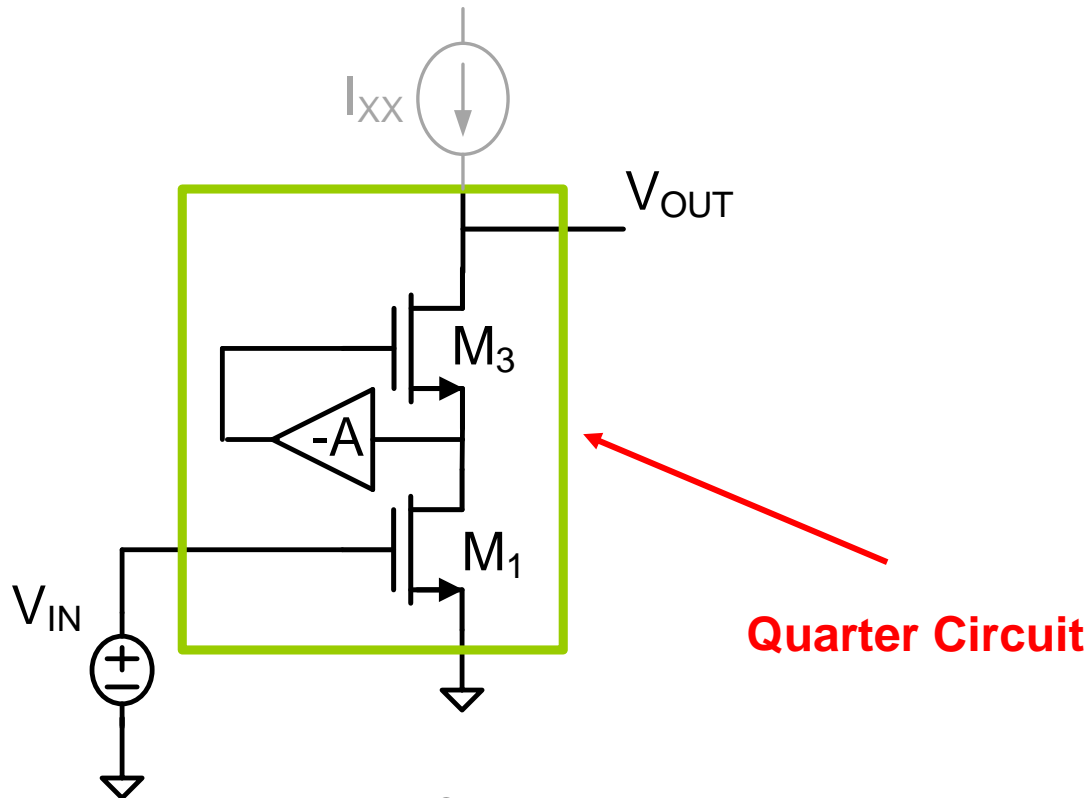


Are there other high output impedance circuits that can be used as quarter circuits ?

Regulated cascode circuits have the high output impedance property



# High output impedance quarter-circuits



**Regulated Cascode Amplifier  
or “Gain Boosted Cascode”**

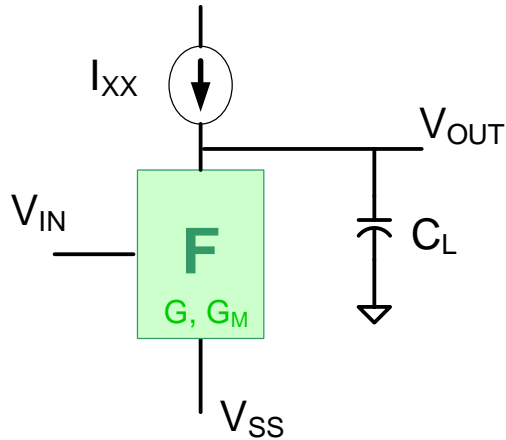
- A is usually a simple amplifier, often the reference op amp with + terminal connected to the desired quiescent voltage
- Assume biased with a dc current source at drain of  $M_3$



Recall: (from earlier lectures)

# Determination of op amp characteristics from quarter circuit characteristics (for single-ended gain)

Small signal Quarter Circuit



$$A_{V_{OQC}} = -\frac{G_M}{G}$$

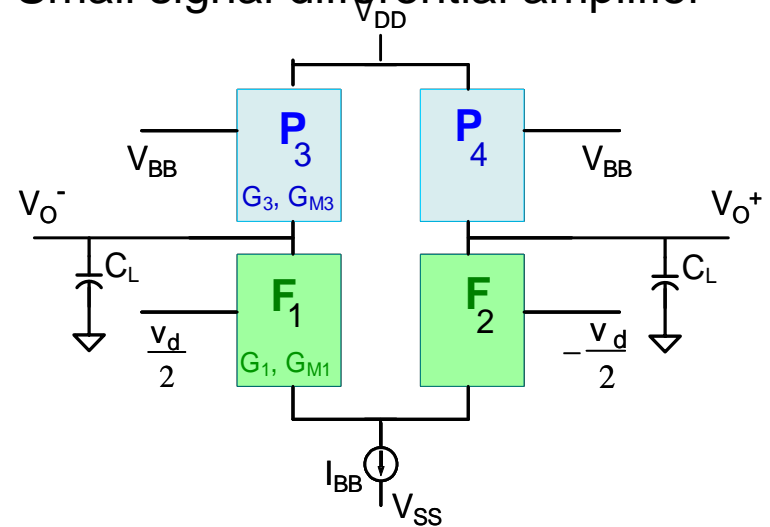
$$BW = \frac{G}{C_L}$$

$$GB = \frac{G_M}{C_L}$$

$$A(s) = \frac{-G_M}{sC_L + G}$$



Small signal differential amplifier



$$A_{V_0} = \frac{-\frac{G_{M1}}{2}}{(G_1 + G_3)}$$

$$BW = \frac{G_1 + G_3}{C_L}$$

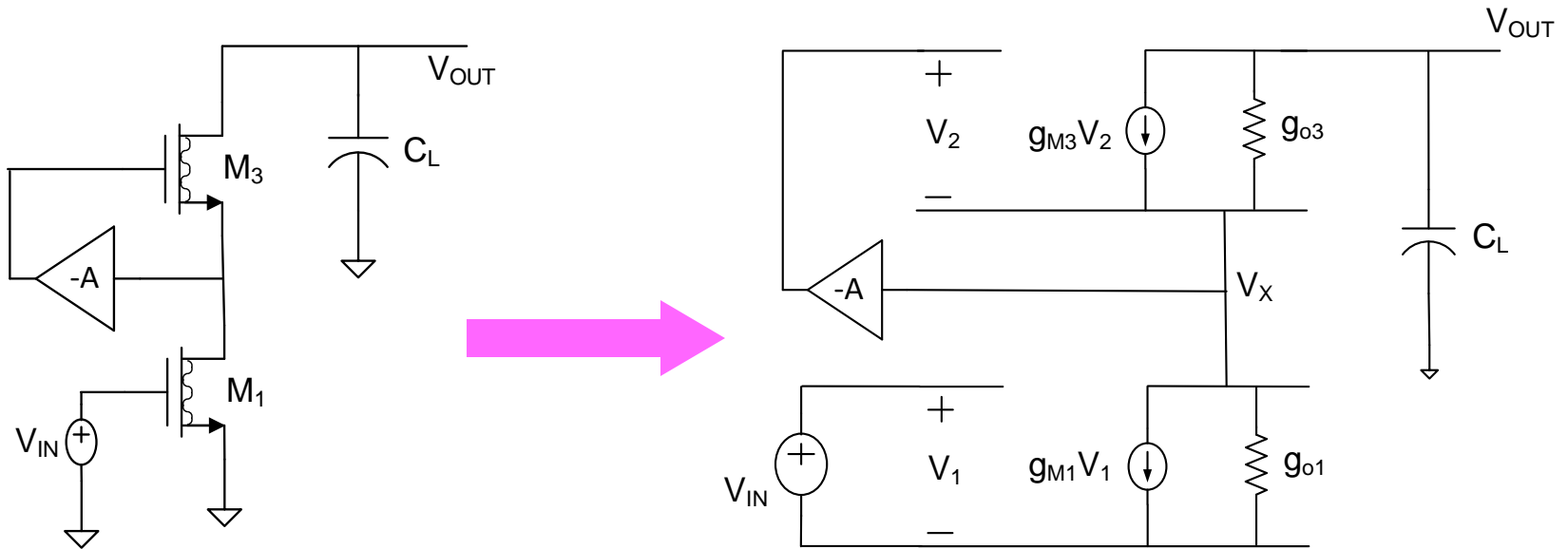
$$GB = \frac{G_{M1}}{2C_L}$$

$$A(s) = \frac{-\frac{G_{M1}}{2}}{sC_L + G_1 + G_3}$$

Note: Factor of 4 reduction of single-ended gain (for  $G_1=G_2$ )

## Background

# Analysis of Regulated Cascode Amplifier

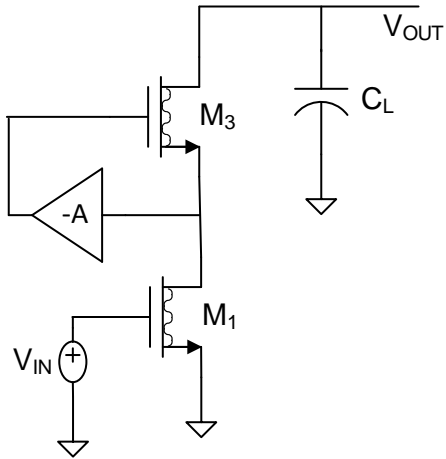


$$\left. \begin{aligned} V_{OUT}(g_{o3} + sC_L) + g_{m3}V_2 &= V_X g_{o3} \\ V_X(g_{o1} + g_{o3}) + g_{m1}V_{IN} - g_{m3}V_2 &= V_{OUT}g_{o3} \\ V_2 + V_X &= -AV_X \end{aligned} \right\}$$

$V_X$  and  $V_2$  can be easily eliminated from these 3 equations

## Background

# Analysis of Regulated Cascode Amplifier



$$\left. \begin{aligned} V_{OUT} (g_{o3} + sC_L) + g_{m3} V_2 &= V_X g_{o3} \\ V_X (g_{o1} + g_{o3}) + g_{m1} V_{IN} - g_{m3} V_2 &= V_{OUT} g_{o3} \\ V_2 + V_X &= -A V_X \end{aligned} \right\}$$

$$\left. \begin{aligned} V_{OUT} (g_{o3} + sC_L) - g_{m3} V_X (1 + A) &= V_X g_{o3} \\ V_X (g_{o1} + g_{o3}) + g_{m1} V_{IN} + g_{m3} V_X (1 + A) &= V_{OUT} g_{o3} \end{aligned} \right\}$$

$$\frac{V_{OUT}}{V_{IN}} = \frac{-g_{m1} (g_{o3} + g_{m3} [1 + A])}{sC_L (g_{o1} + g_{o3} + g_{m3} [1 + A]) + g_{o1} g_{o3}} \approx \frac{-g_{m1} g_{m3} [1 + A]}{sC_L g_{m3} [1 + A] + g_{o1} g_{o3}} = \frac{-g_{m1}}{sC_L + \frac{g_{o1} g_{o3}}{g_{m3} [1 + A]}}$$

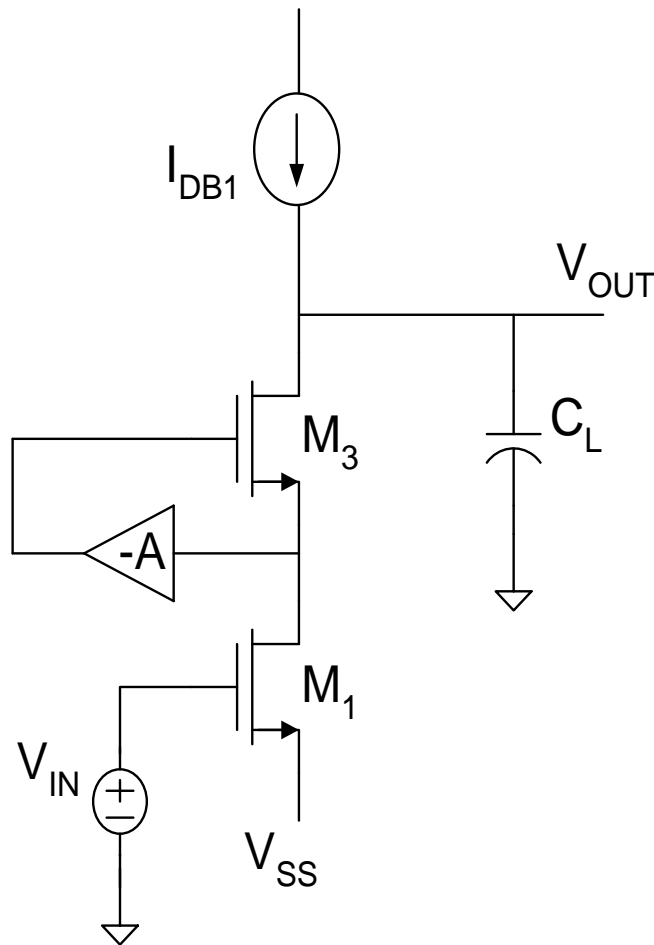
for A large:

$$\frac{V_{OUT}}{V_{IN}} \approx \frac{-g_{m1}}{sC_L + g_{o1} \left( \frac{g_{o3}}{g_{m3}} \right) \left( \frac{1}{A} \right)}$$

$g_{MEQ}$  alt  $G_M$

$g_{OEQ}$  alt  $G$

# High output impedance quarter-circuits



**Regulated Cascode Amplifier  
or “Gain Boosted Cascode”**

$$g_{OEQ} \cong g_{o1} \left[ \frac{g_{o3}}{g_{m3}} \frac{1}{A} \right]$$

$$g_{mEQ} \cong g_{m1}$$

Based upon small-signal analysis it appears that the output conductance has been decreased even more!

$$A_V \cong \frac{-g_{m1}}{sC_L + g_{o1} \left( \frac{g_{o3}}{g_{m3} A} \right)}$$

$$A_O \cong -\frac{g_{m1}}{g_{o1}} \bullet \left[ \frac{g_{m3} A}{g_{o3}} \right]$$

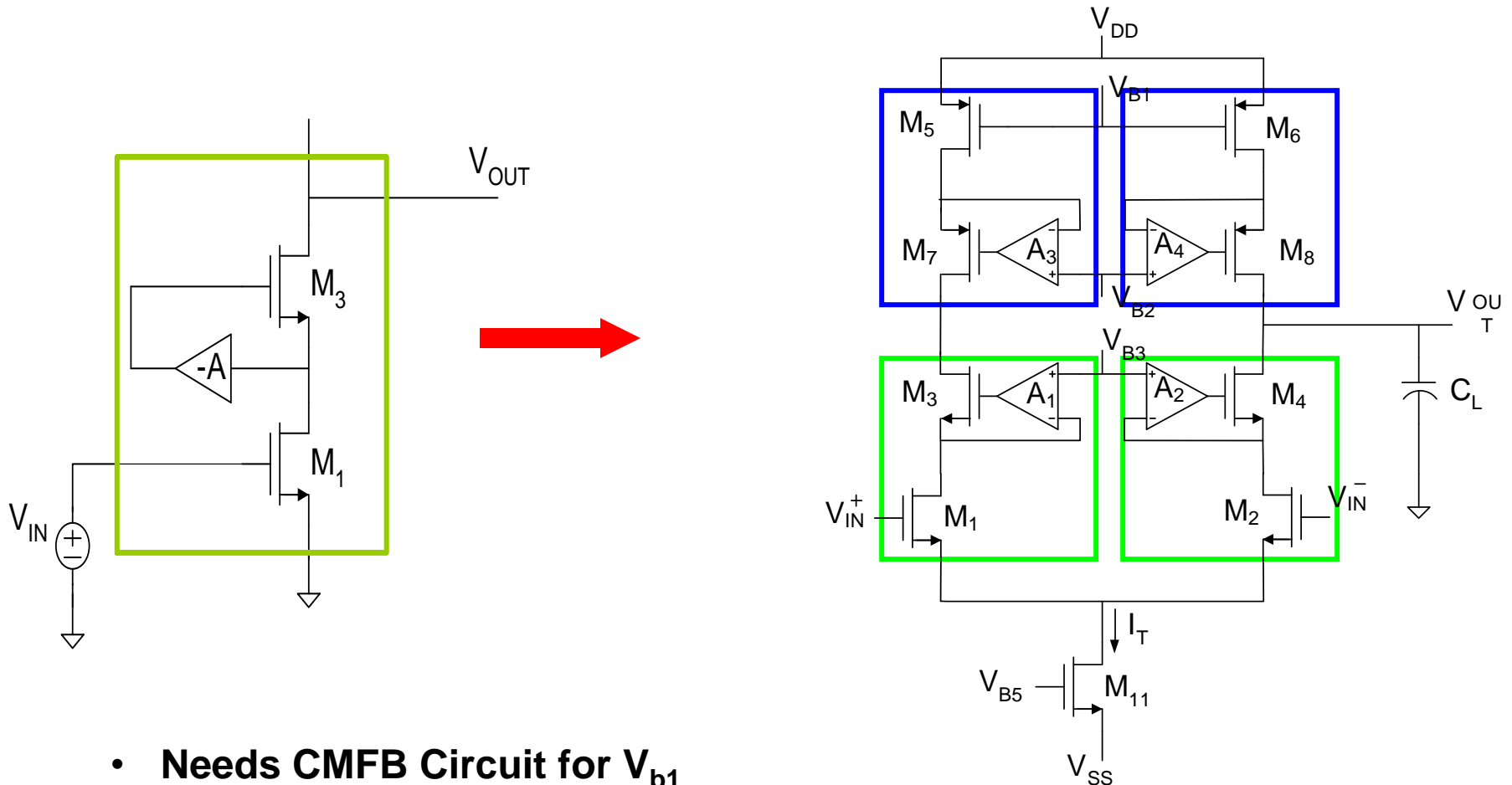
$$GB \cong \frac{g_{m1}}{C_L}$$

Same GB as for previous two circuits

Must verify improvement in gain in practical parameter domain !!

Verification will show predicted improvements

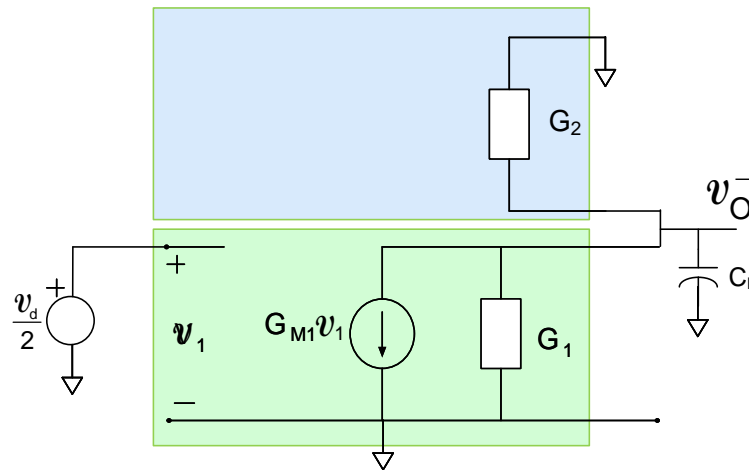
# Gain-Boosted Telescopic Cascode Op Amp



- Needs CMFB Circuit for  $V_{b1}$
- Either single-ended or differential outputs
- Can connect counterpart as current mirror to eliminate CMFB
- Use differential op amp to facilitate biasing of cascode device

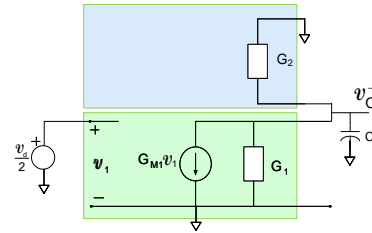
# Recall from earlier lecture:

-- The “differential” gain --



$$A_{Vd} = \frac{v_o^-}{v_d} = \frac{-\frac{G_{M1}}{2}}{sC_L + G_1 + G_2}$$

# Gain-Boosted Telescopic Cascode Op Amp



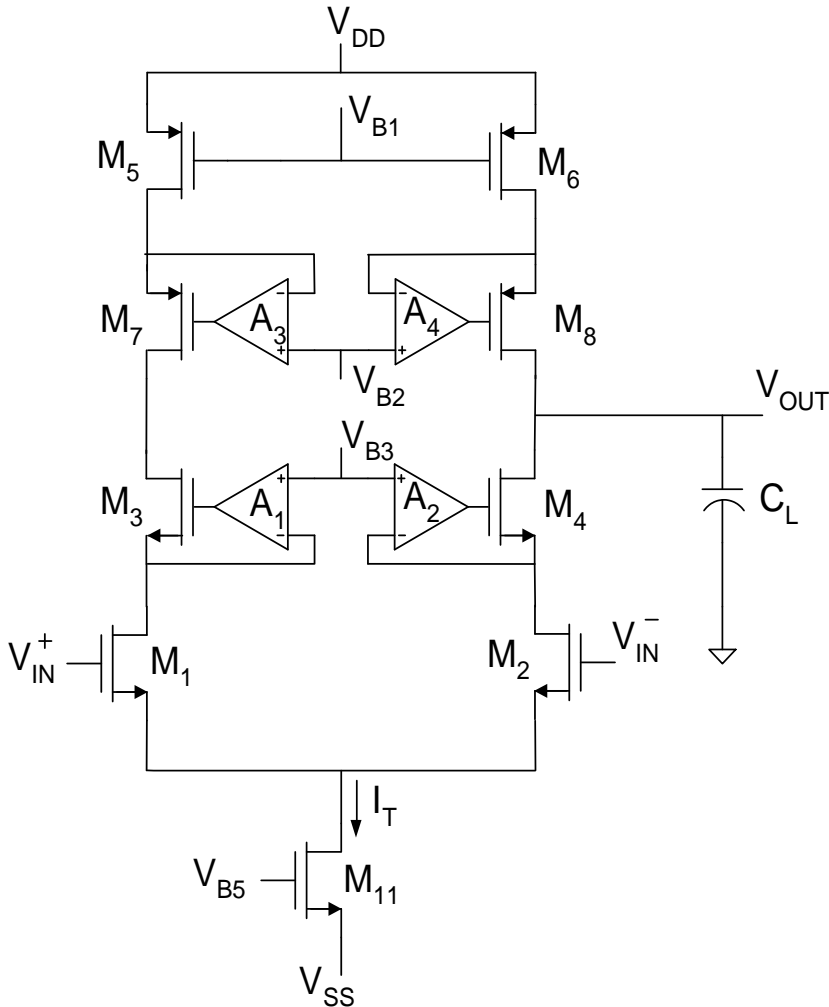
$$A_{Vd} = \frac{v_o^-}{v_d} = \frac{-\frac{G_{M1}}{2}}{sC_L + G_1 + G_2}$$

## Single-ended operation

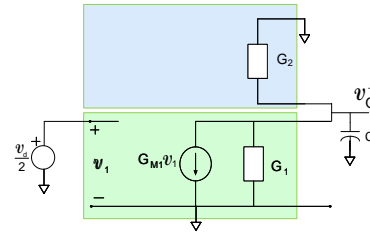
$$G_1 = g_{OQC} = \underline{\hspace{10em}}$$

$$G_2 = g_{OCC} = \underline{\hspace{10em}}$$

$$G_{M1} = g_{mQC} = \underline{\hspace{10em}}$$



# Gain-Boosted Telescopic Cascode Op Amp



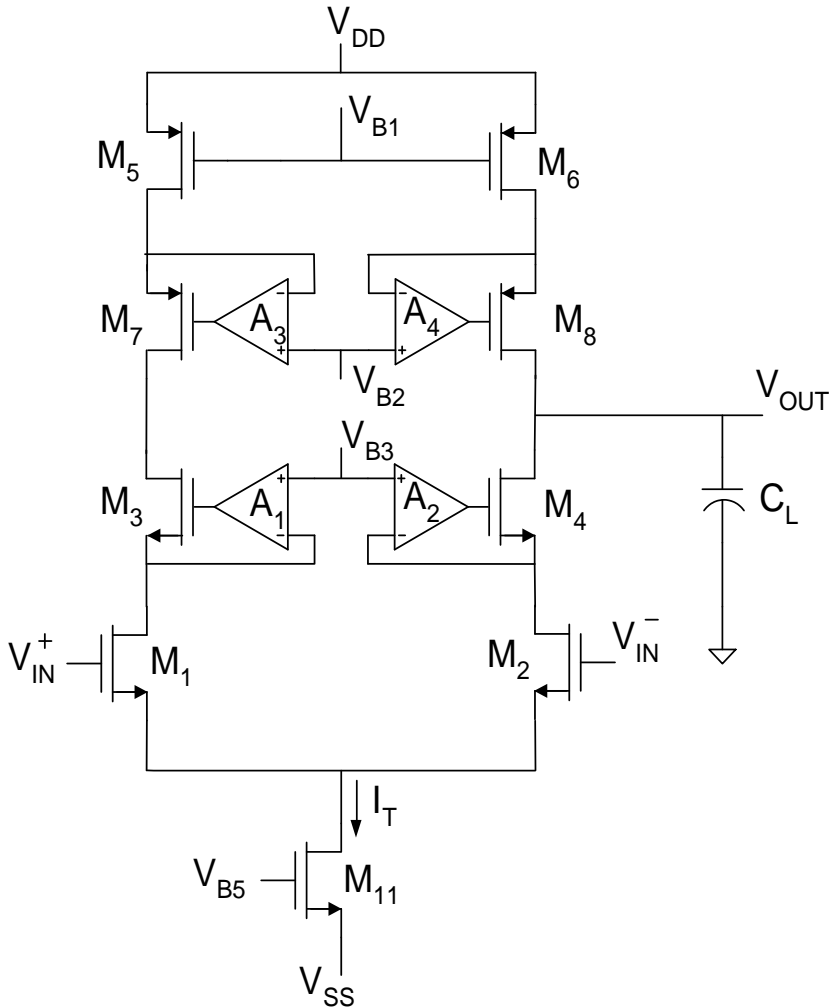
$$A_{Vd} = \frac{v_o^-}{v_d} = \frac{-\frac{G_{M1}}{2}}{sC_L + G_1 + G_2}$$

## Single-ended operation

$$G_1 = g_{OQC} = g_{o1} \frac{g_{o3}}{g_{m3}} \frac{1}{A_1}$$

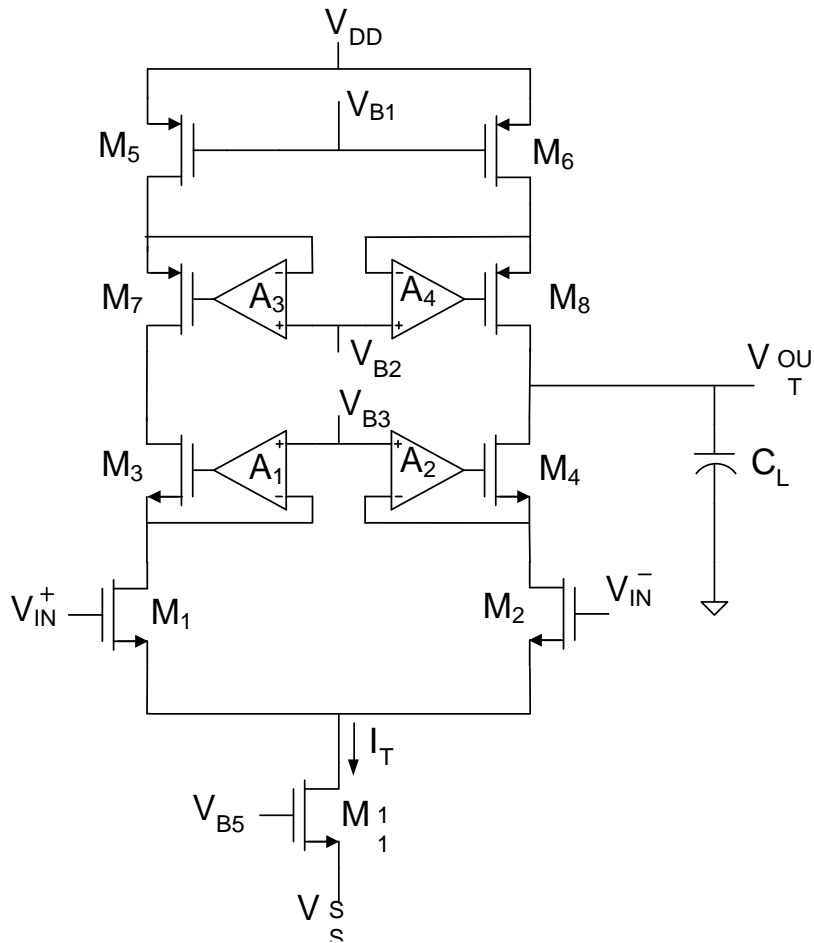
$$G_2 = g_{OCC} = g_{o5} \frac{g_{o7}}{g_{m7}} \frac{1}{A_3}$$

$$G_{M1} = g_{mQC} = g_{m1}$$



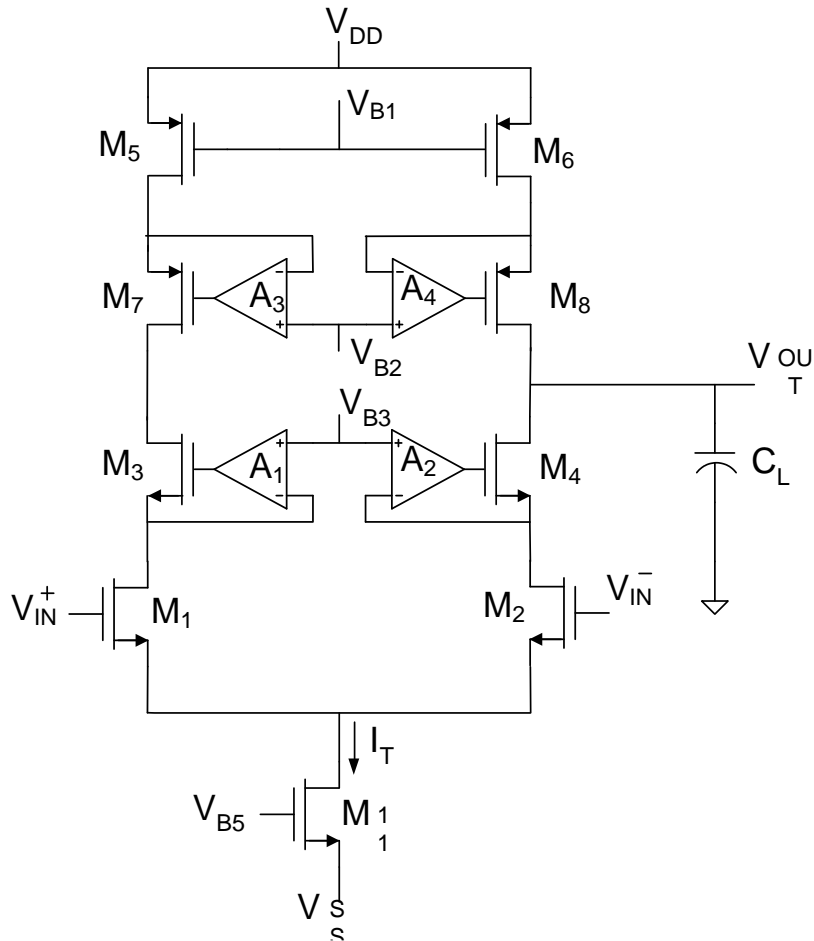


# Gain-Boosted Telescopic Cascode Op Amp



$$A(s) = \frac{-\frac{g_{m1}}{2}}{sC_L + g_{o1} \frac{g_{o3}}{A_1 g_{m3}} + g_{o5} \frac{g_{o7}}{A_3 g_{m7}}}$$

# Gain-Boosted Telescopic Cascode Op Amp



$$A(s) = \frac{-g_{m1}}{2} \frac{1}{sC_L + g_{o1} \frac{g_{o3}}{A_1 g_{m3}} + g_{o5} \frac{g_{o7}}{A_3 g_{m7}}}$$



$$A_o = \frac{-g_{m1}}{2} \frac{1}{g_{o1} \frac{g_{o3}}{A_1 g_{m3}} + g_{o5} \frac{g_{o7}}{A_3 g_{m7}}}$$

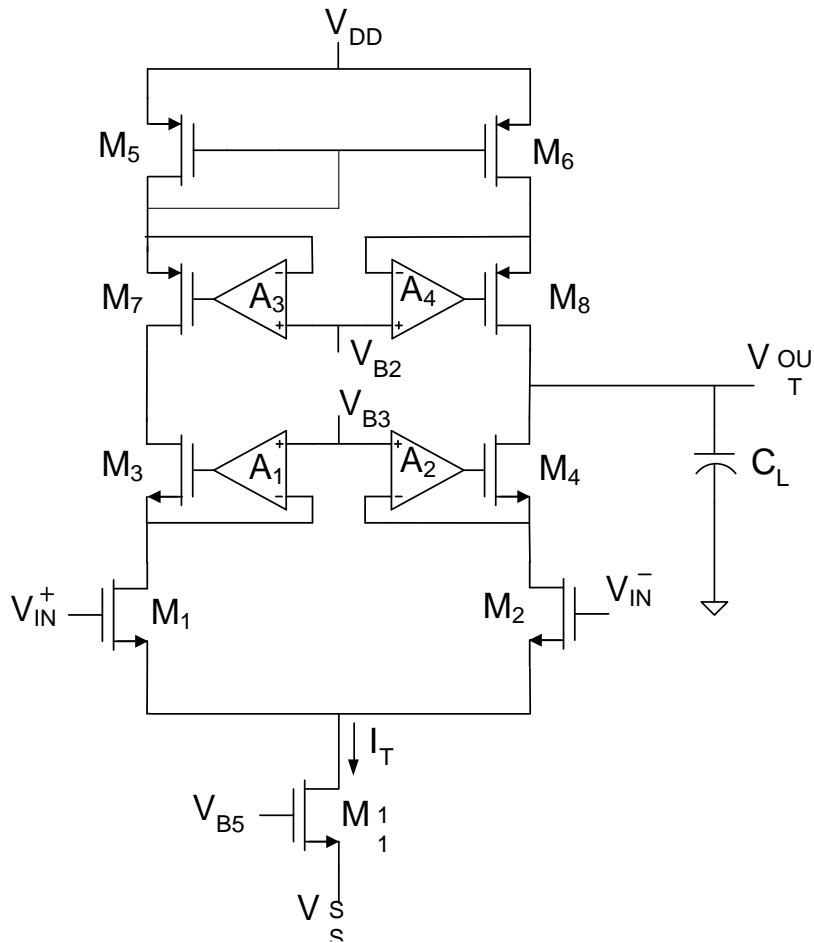
$$BW = \frac{g_{o1} \frac{g_{o3}}{A_1 g_{m3}} + g_{o5} \frac{g_{o7}}{A_3 g_{m7}}}{C_L}$$

$$GB \approx \frac{g_{m1}}{2C_L}$$

This is modestly less efficient at generating GB because now power is consumed in the boosting amplifiers as well

# Gain-Boosted Telescopic Cascode Op Amp

## with Counterpart Current Mirror



$$A_o = \frac{-g_{m1}}{g_{o1} \frac{g_{o3}}{A_1 g_{m3}} + g_{o5} \frac{g_{o7}}{A_3 g_{m7}}}$$

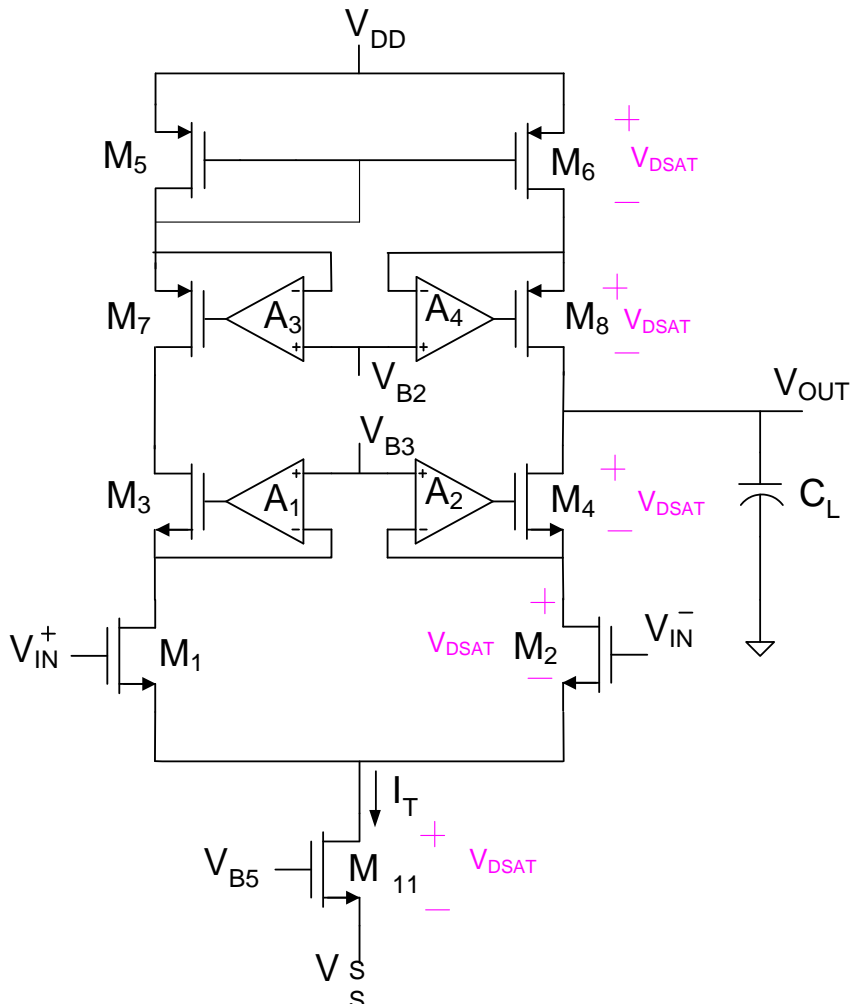
$$GB = \frac{g_{m1}}{C_L}$$

This is modestly less efficient at generating GB because now power is consumed in the boosting amplifiers as well

Elimination of need for CMFB Circuit

# Gain-Boosted Telescopic Cascode Op Amp

## Signal Swing and Power Supply Limitations



A minimum of  $5 V_{DSAT}$  drops  
 $+V_{TH}$  between  $V_{DD}$  and  $V_{SS}$

This establishes a lower bound  
on  $V_{DD}-V_{SS}$  and it will be reduced  
by the p-p signal swing on the  
output

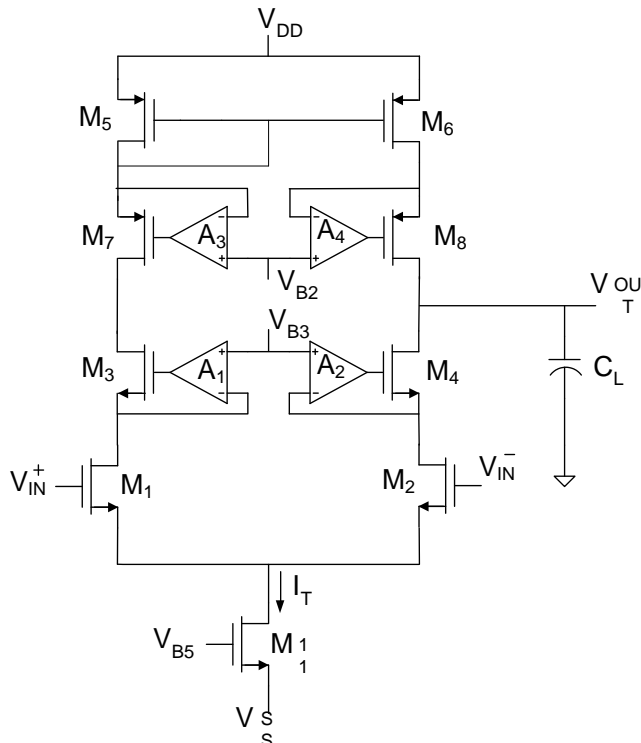
# Gain-Boosted Telescopic Cascode Op Amp

(with or w/o current mirror counterpart circuits)

Advantages:

Significant increase in dc gain

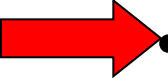
Limitations:



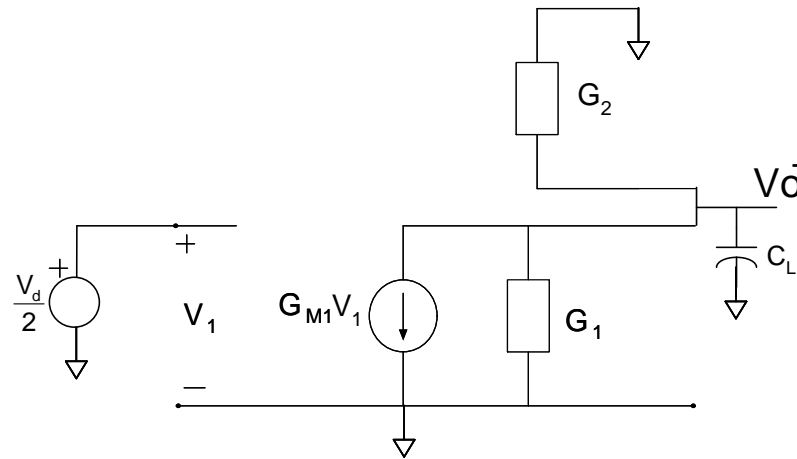
- Signal swing ( $5V_{DSAT} + V_{TH}$  between  $V_{DD}$  and  $V_{SS}$ )
- Reduction in GB power efficiency
  - some current required to bias “A” amplifiers
- -additional pole in “A” amplifier
  - may add requirements for some compensation
- Area Overhead for 4 transistors and 4 amplifiers
  - actually minor concern since performance will usually justify these resources

Where we are at:

# Basic Op Amp Design

- Fundamental Amplifier Design Issues
- Single-Stage Low Gain Op Amps
-  • Single-Stage High Gain Op Amps
- Other Basic Gain Enhancement Approaches
- Two-Stage Op Amp

Are there other useful high output impedance circuits that can be used for the quarter circuit?

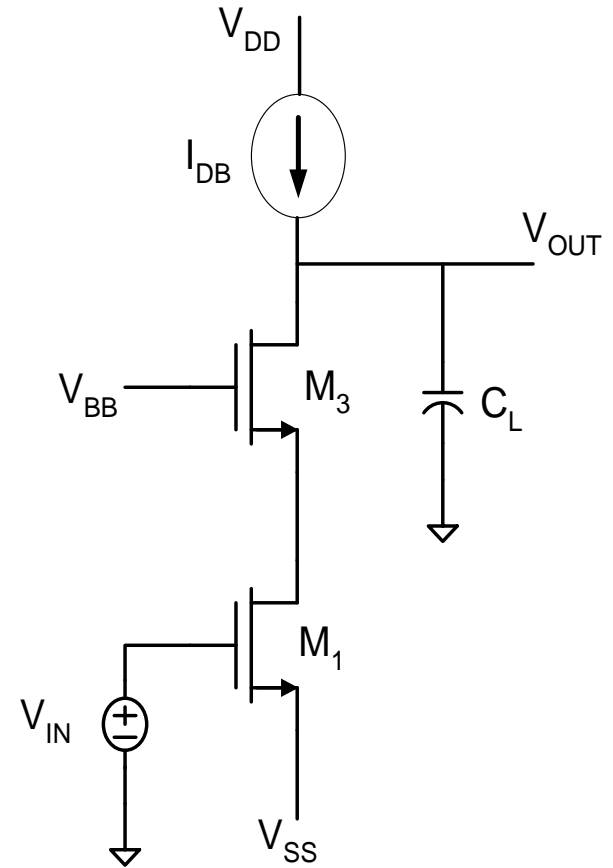
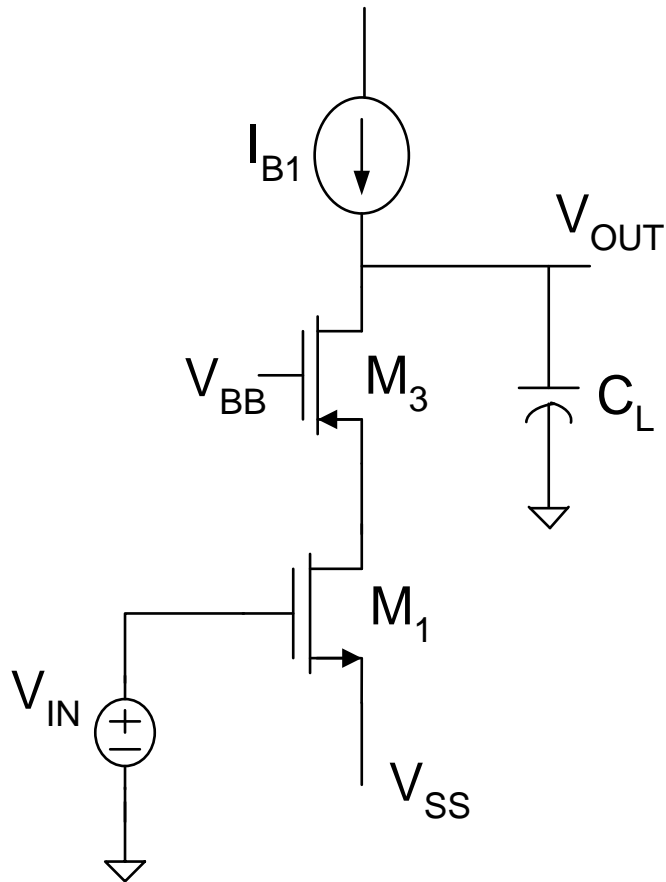


$$A_{V_0} = \frac{-G_{M1}}{2(G_1 + G_2)}$$

$$BW = \frac{G_1 + G_2}{C_L}$$

$$GB = \frac{G_{M1}}{2C_L}$$

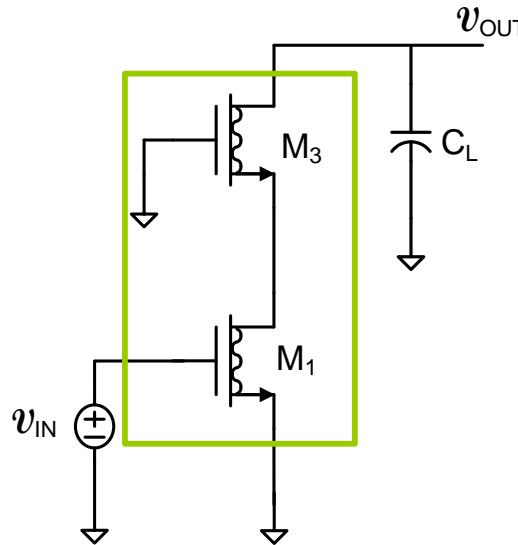
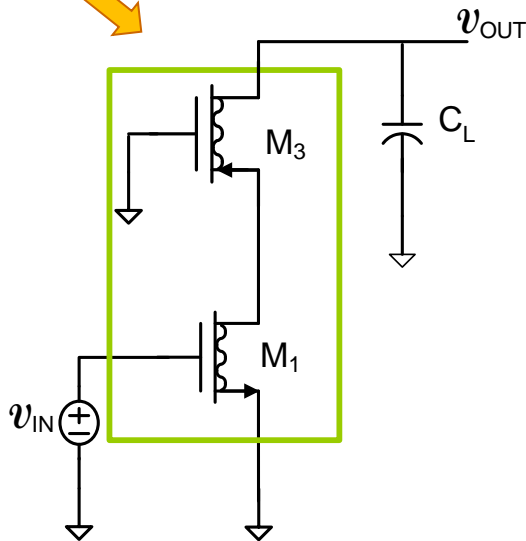
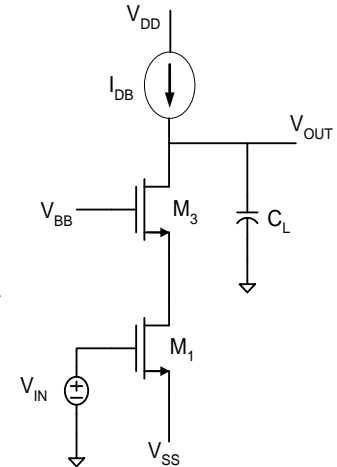
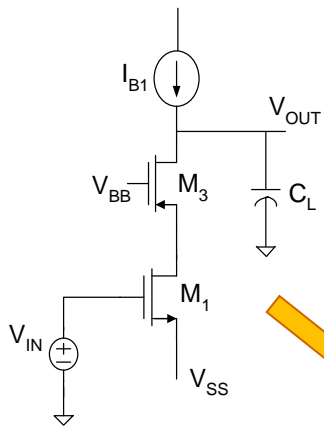
# What circuit is this?



Cascode Amplifier



# What circuit is this?



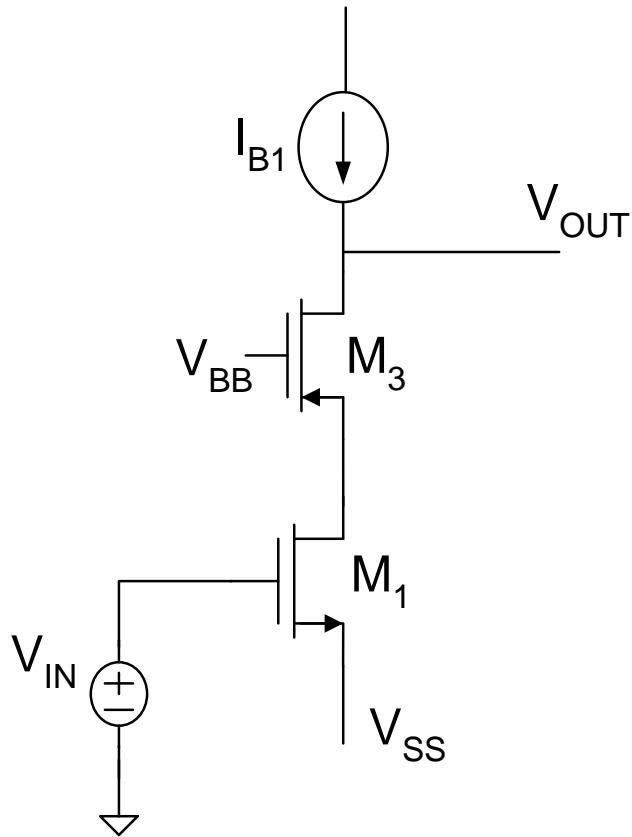
Small-signal circuit structures are identical !

- Cascode Amplifier

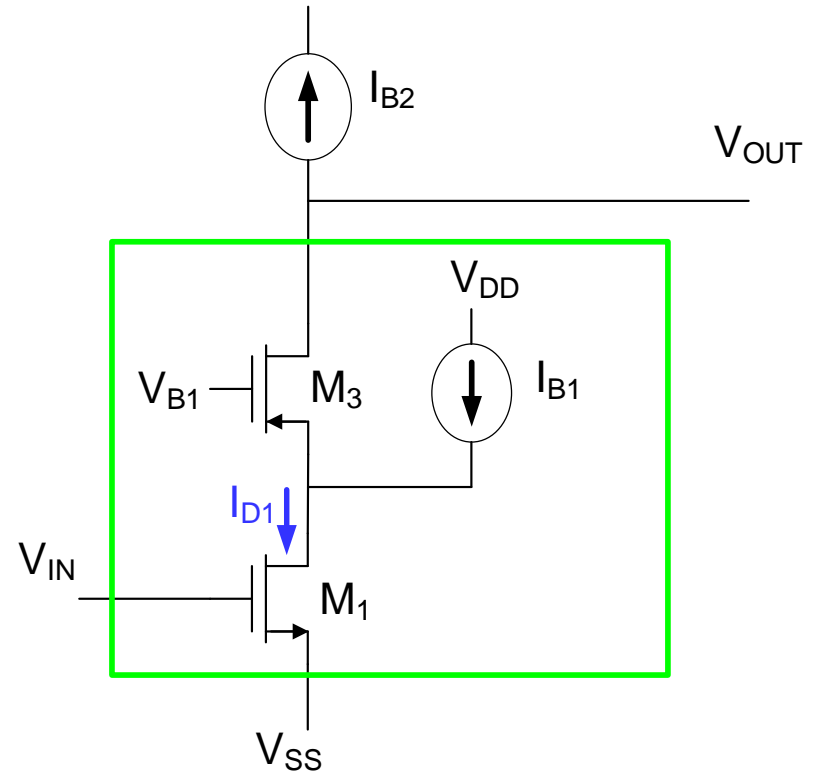
- Often termed a “Folded Cascode Amplifier”
- Same small-signal performance as other
- $V_{OUT}$  swing  $V_{DSAT1} - V_{DSAT2}$  could be small or negative
- **But a biasing problem !!**

## Cascode Amplifier

# Biased Folded Cascode Amplifier



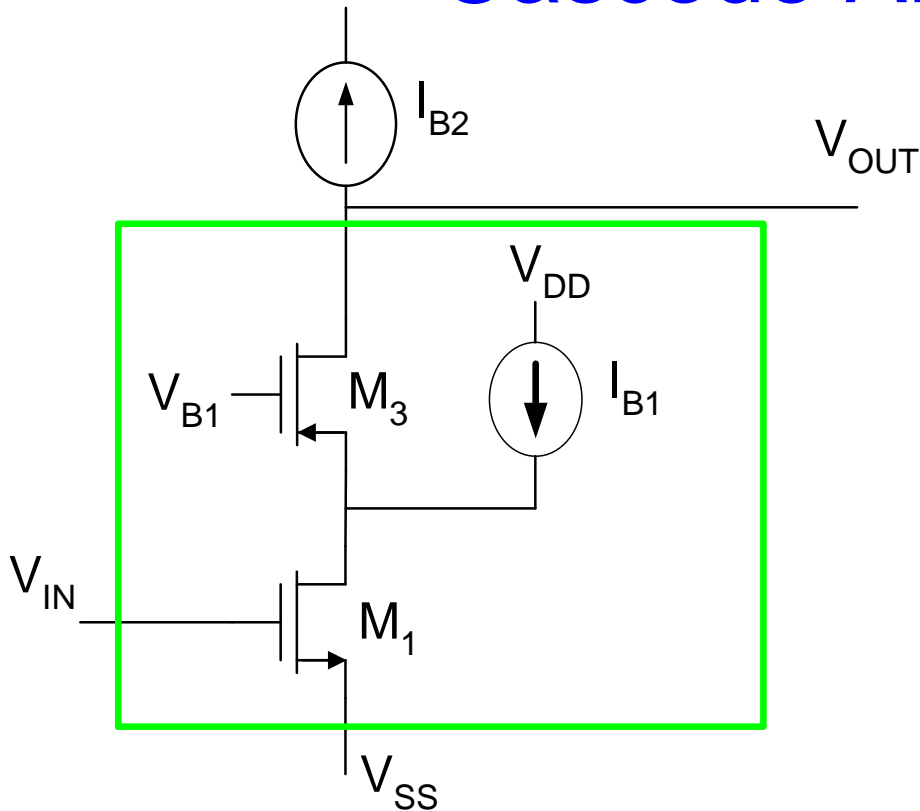
**Folded Cascode Amplifier**



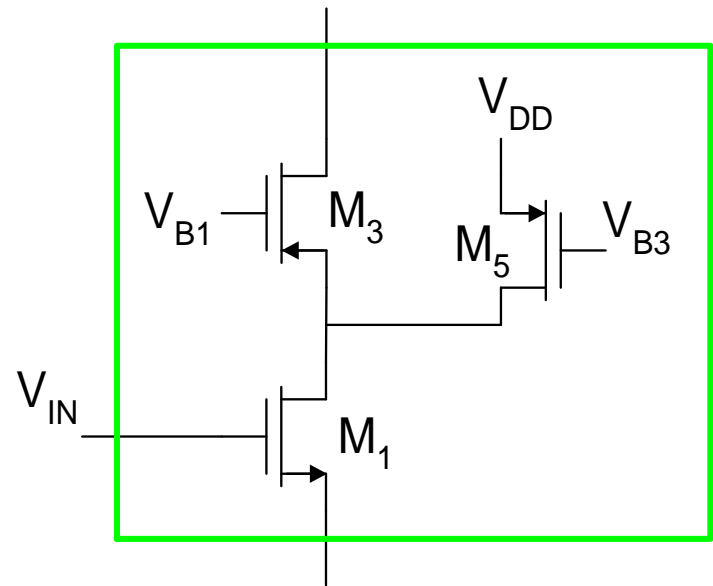
**Biased Folded Cascode**

Must have  $I_{D1} = I_{B1} - I_{B2} > 0$

# Implementation of Biased Folded Cascode Amplifier?

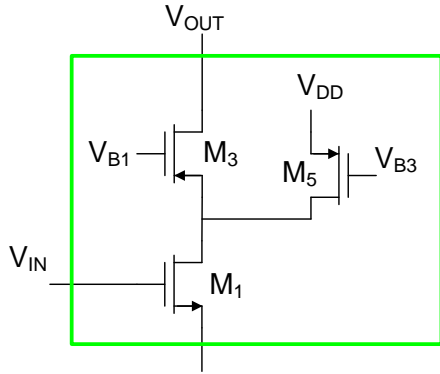


**Biased Folded Cascode**



**Implementation of Biased Folded Cascode**

# Analysis of Biased Folded Cascode



with ideal dc bias current in drain of  $M_2$  (not shown)

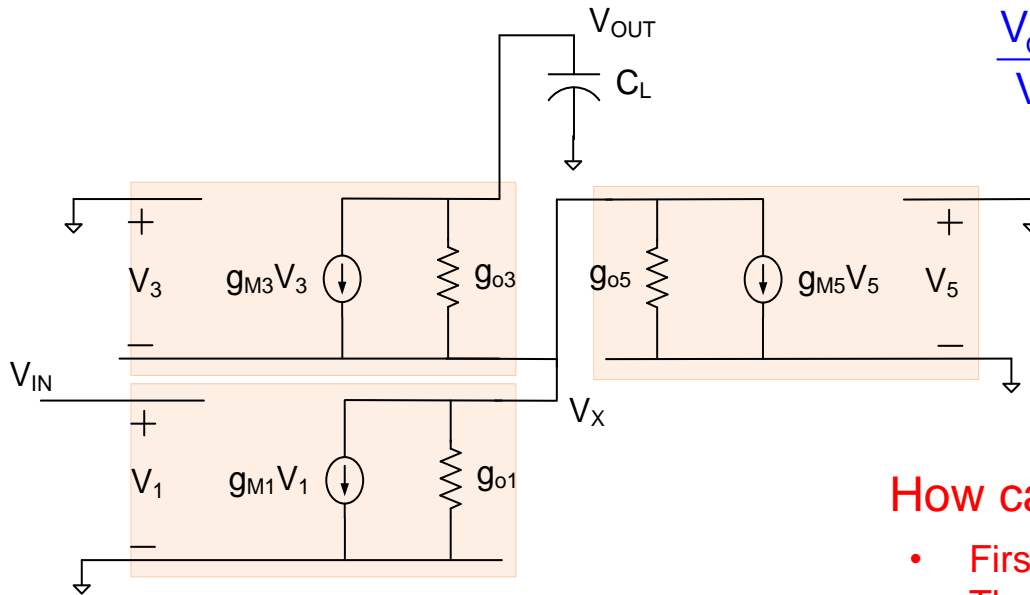
$$A_{Vd} = \frac{v_o}{v_{IN}} = \frac{-G_M}{sC_L + G}$$

$$\left. \begin{aligned} V_{OUT} (g_{o3} + sC_L) + g_{m3} V_3 &= V_X g_{o3} \\ V_X (g_{o1} + g_{o3} + g_{o5}) + g_{m1} V_1 - g_{m3} V_3 &= V_{OUT} g_{o3} \\ V_3 &= -V_X \\ V_1 &= V_{IN} \end{aligned} \right\}$$

$$\left. \begin{aligned} V_{OUT} (g_{o3} + sC_L) + (g_{m3} + g_{o3}) V_3 &= 0 \\ +g_{m1} V_{IN} &= V_3 (g_{m3} + g_{o1} + g_{o3} + g_{o5}) + V_{OUT} g_{o3} \end{aligned} \right\}$$

$$\frac{V_{OUT}}{V_{IN}} \cong - \frac{g_{m1}}{sC_L + (g_{o1} + g_{o5}) \frac{g_{o3}}{g_{m3}}} G_M$$

**G**



How can this be seen by inspection?

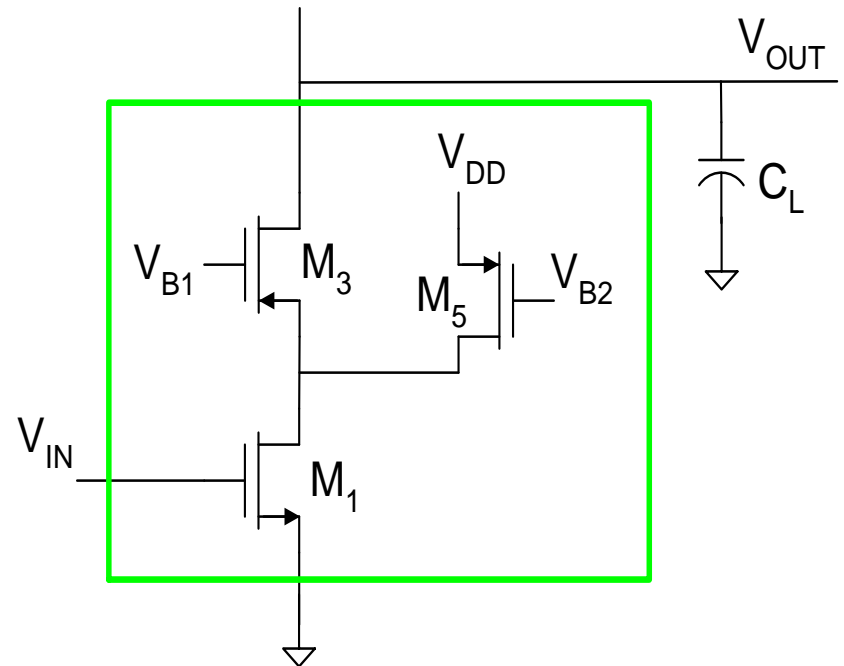
- First observe if all  $g_o$ 's are 0,  $G_M = g_{m1}$
- Then observe  $M_3$  "cascode" the impedance  $g_{o1} + g_{o5}$

# Biased Folded Cascode Quarter Circuit

$$\frac{V_{OUT}}{V_{IN}} \cong - \frac{g_{m1}}{sC_L + (g_{o1} + g_{o5}) \frac{g_{o3}}{g_{m3}}}$$

$$A_{v0} \cong \frac{g_{m1}}{(g_{o1} + g_{o5})} \frac{g_{m3}}{g_{o3}}$$

$$GB \cong \frac{g_{m1}}{C_L}$$



# Basic Amplifier Structure Comparisons

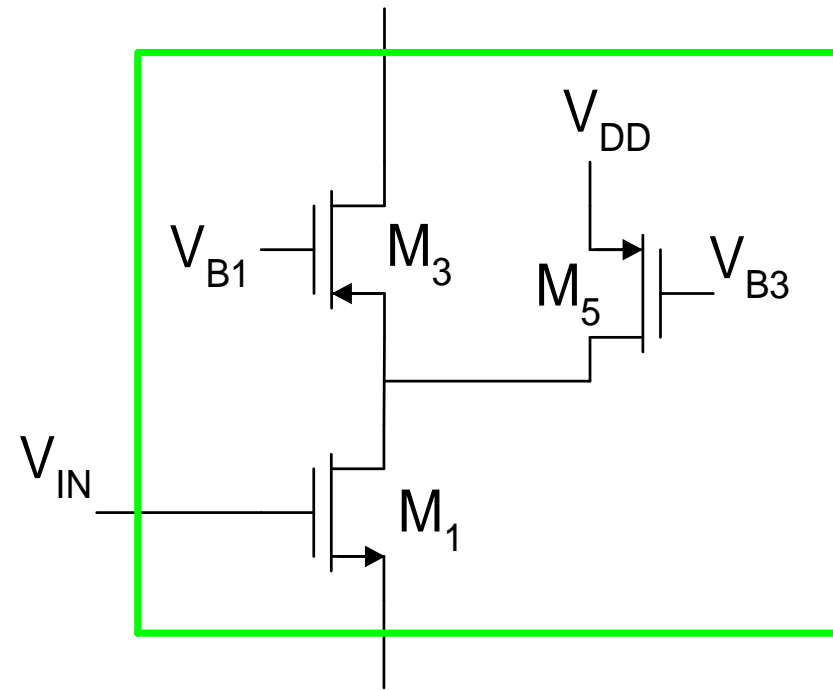
(ideal current source biasing)

Small Signal Parameter Domain		
Common Source	$A_{v0} \approx \frac{g_m}{g_o}$	$GB \approx \frac{g_m}{C_L}$
Cascode	$A_{v0} \approx \frac{g_{m1}}{g_{o1}} \frac{g_{m3}}{g_{o3}}$	$GB \approx \frac{g_m}{C_L}$
Regulated Cascode	$A_{v0} \approx \frac{g_{m1}}{g_{o1}} \frac{g_{m3}}{g_{o3}} A$	$GB \approx \frac{g_m}{C_L}$
Folded Cascode	$A_{v0} \approx \frac{g_{m1}}{(g_{o1} + g_{o5})} \frac{g_{m3}}{g_{o3}}$	$GB \approx \frac{g_m}{C_L}$

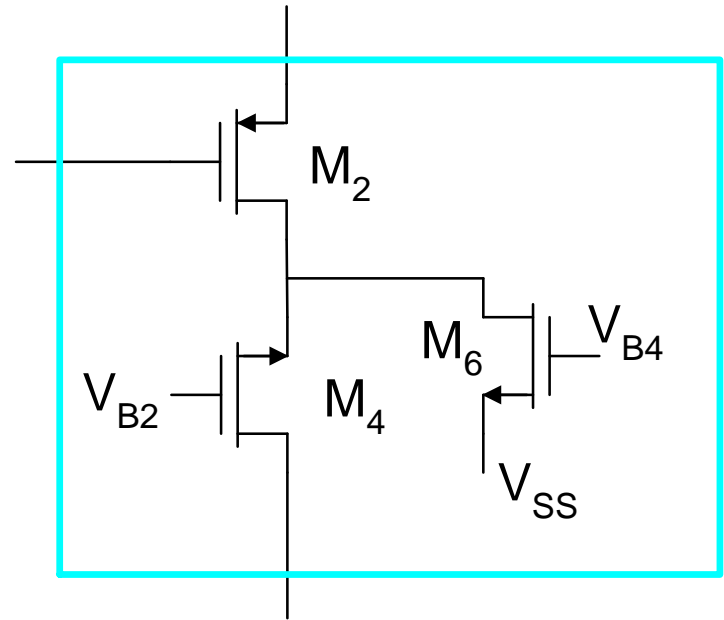
# Basic Amplifier Structure Comparisons

Practical Parameter Domain		
Common Source	$A_{VO} = \left( \frac{2}{\lambda} \right) \left( \frac{1}{V_{EB}} \right)$	$GB = \left( \frac{2P}{V_{DD} C_L} \right) \left( \frac{1}{V_{EB}} \right)$
Cascode	$A_{VO} = \left( \frac{4}{\lambda_1 \lambda_3} \right) \left( \frac{1}{V_{EB1} V_{EB3}} \right)$	$GB = \left( \frac{2P}{V_{DD} C_L} \right) \left( \frac{1}{V_{EB1}} \right)$
Regulated Cascode $\Theta$ =pct power in A	$A_{VO} \approx \left( \frac{4}{\lambda_1 \lambda_3} \right) \left( \frac{A}{V_{EB1} V_{EB3}} \right)$	$GB = \left( \frac{2P}{V_{DD} C_L} \right) \left( \frac{(1-\Theta)}{V_{EB1}} \right)$
Folded Cascode $\Theta$ =fraction of current of $M_5$ that is in $M_1$	$A_{VO} \approx \left( \frac{4\Theta}{(\Theta\lambda_1 + \lambda_5)\lambda_3 V_{EB1} V_{EB3}} \right)$	$GB = \left( \frac{2P}{V_{DD} C_L} \right) \left[ \frac{\Theta}{V_{EB1}} \right]$

# Biased Folded-Cascode Amplifier



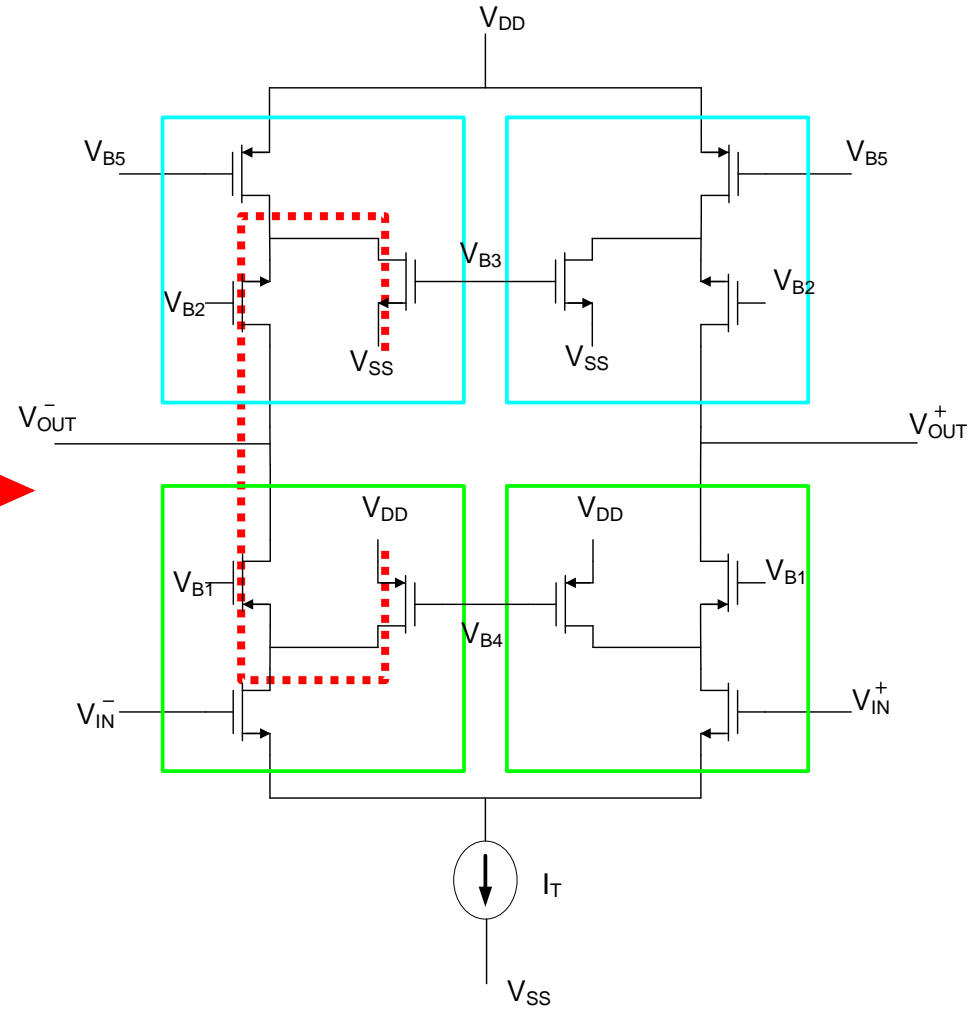
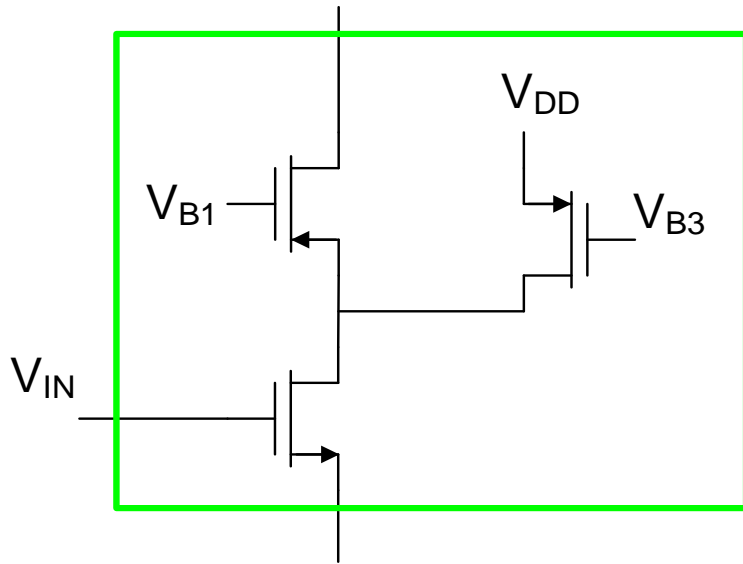
Quarter Circuit



Counterpart Circuit



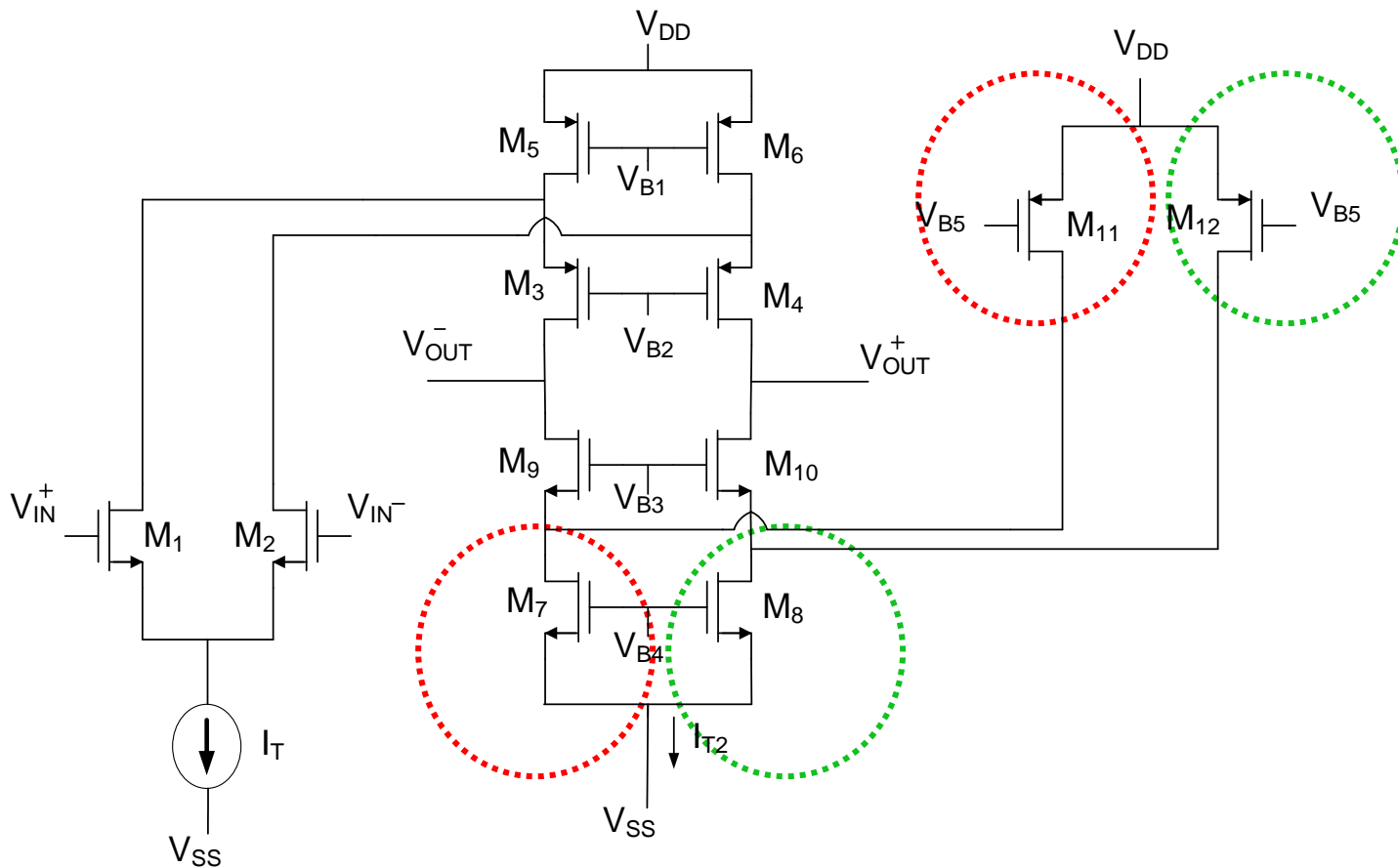
# Folded-Cascode Operational Amplifier



**QUARTER CIRCUIT**

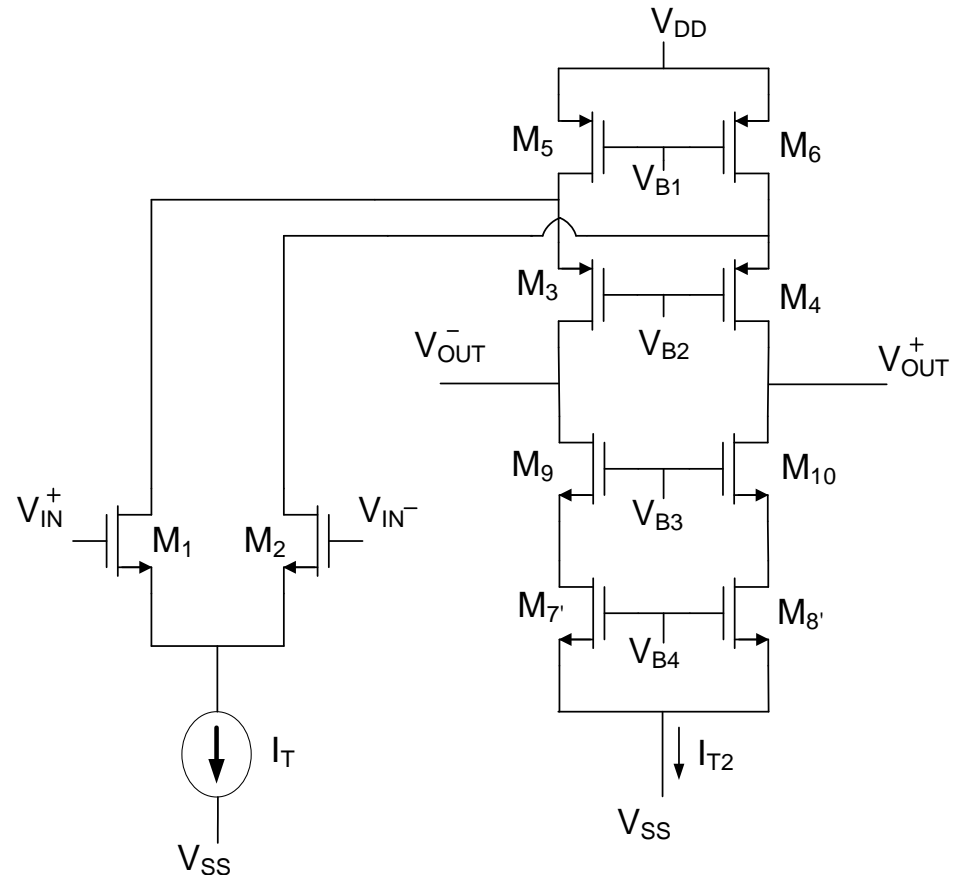
**Op Amp**

# Folded-Cascode Operational Amplifier (redrawn)



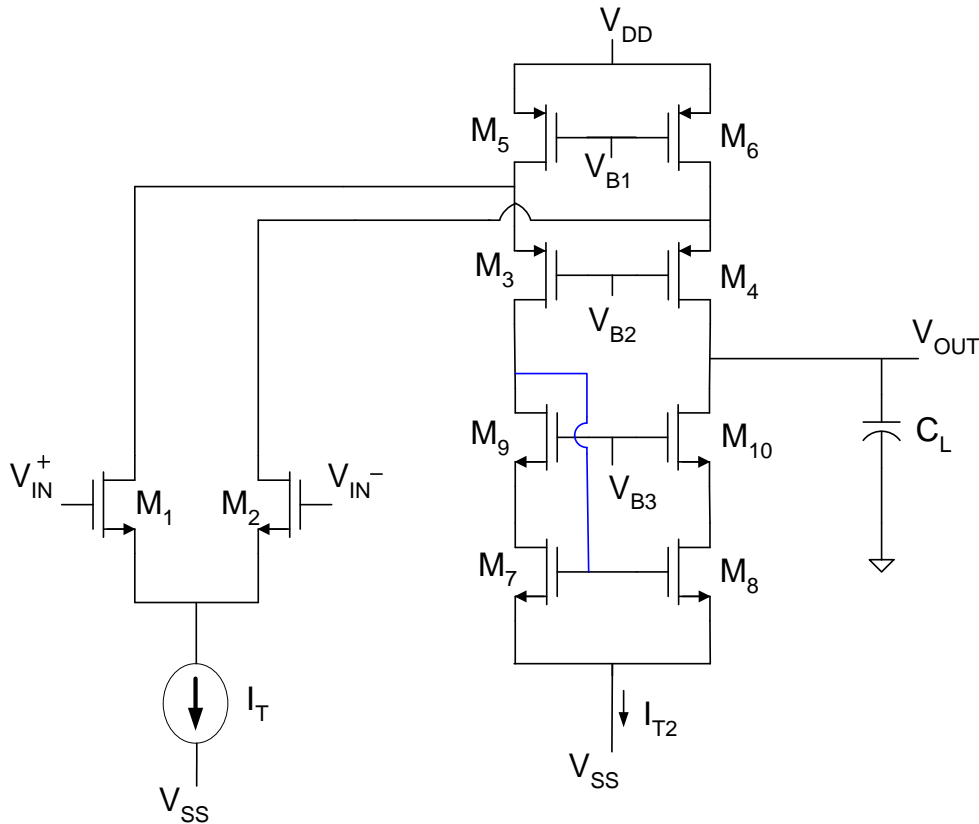
These transistors pair-wise form a current source and one in each pair can be removed

# Folded Cascode Op Amp



- Needs CMFB Circuit for  $V_{B4}$
- Either single-ended or differential outputs
- Can connect counterpart as current mirror to eliminate CMFB
- Folding caused modest deterioration of  $A_{v0}$  and GB energy efficiency
- Modest improvement in output swing

# Folded Cascode Op Amp (Single-ended Output)



$$A_V(s) \approx - \frac{g_{mEQ}}{sC_L + g_{OEQ}}$$

$$A_{V0} \approx \frac{g_{mEQ}}{g_{OEQ}}$$

$$GB \approx \frac{g_{mEQ}}{C_L}$$

$$g_{mEQ} = g_{m1}$$

$$g_{OEQ} \approx (g_{O1} + g_{O5}) \frac{g_{O3}}{g_{m3}} + (g_{O7}) \frac{g_{O9}}{g_{m9}}$$

$$A_{V0} \approx \frac{g_{m1}}{(g_{O1} + g_{O5}) \frac{g_{O3}}{g_{m3}} + (g_{O7}) \frac{g_{O9}}{g_{m9}}}$$

$$GB = \frac{g_{m1}}{C_L}$$

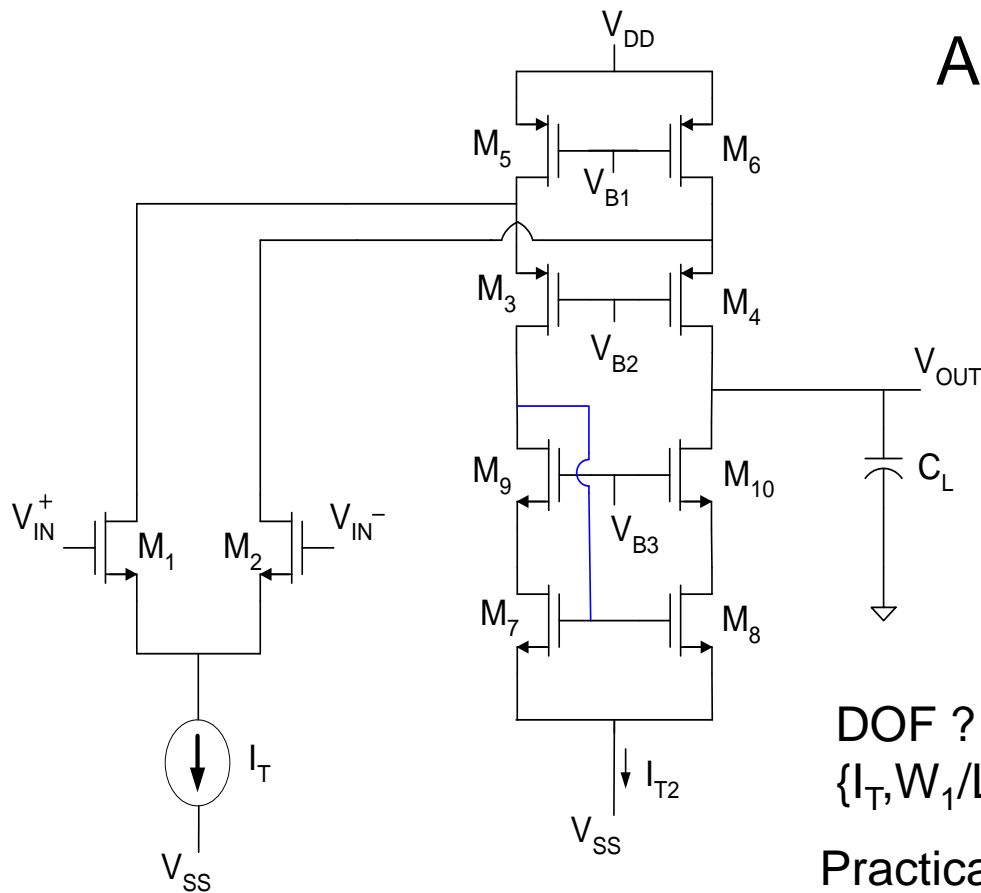
# Operational Amplifier Structure Comparison

Small Signal Parameter Domain			
Reference Op Amp	$A_{vo} = \frac{1}{2} \frac{g_{m1}}{g_{o1} + g_{o3}}$	$GB = \frac{g_{m1}}{2C_L}$	$SR = \frac{I_T}{2C_L}$
Telescopic Cascode	$A_o = \frac{\frac{g_{m1}}{2}}{g_{o1} \frac{g_{o3}}{g_{m3}} + g_{o7} \frac{g_{o5}}{g_{m5}}}$	$GB = \frac{g_{m1}}{2C_L}$	$SR = \frac{I_T}{2C_L}$
Regulated Cascode	$A_o \approx \frac{\frac{g_{m1}}{2}}{g_{o1} \frac{g_{o3}}{g_{m3} A_1} + g_{o7} \frac{g_{o9}}{g_{m9} A_3}}$	$GB = \frac{g_{m1}}{2C_L}$	$SR = \frac{I_T}{2C_L}$
Folded Cascode	$A_o = \frac{\frac{g_{m1}}{2}}{(g_{o1} + g_{o5}) \frac{g_{o3}}{g_{m3}} + g_{o7} \frac{g_{o9}}{g_{m9}}}$	$GB = \frac{g_{m1}}{2C_L}$	$SR = \frac{I_T}{2C_L}$

# Operational Amplifier Structure Comparison

Practical Parameter Domain			
Reference Op Amp	$A_{V0} = \left[ \frac{1}{\lambda_1 + \lambda_3} \right] \left( \frac{1}{V_{EB1}} \right)$	$GB = \left( \frac{P}{2V_{DD}C_L} \right) \cdot \left[ \frac{1}{V_{EB1}} \right]$	$SR = \frac{P}{2V_{DD}C_L}$
Telescopic Cascode	$A_{V0} = \frac{2}{V_{EB1}(\lambda_1\lambda_3V_{EB3} + \lambda_5\lambda_7V_{EB5})}$	$GB = \left( \frac{P}{2V_{DD}C_L} \right) \cdot \left[ \frac{1}{V_{EB1}} \right]$	$SR = \frac{P}{2V_{DD}C_L}$
Regulated Cascode $\Theta$ =pct power in A	$A_{V0} \approx \frac{2}{V_{EB1} \left( \frac{\lambda_1\lambda_3V_{EB3}}{A_1} + \frac{\lambda_5\lambda_7V_{EB7}}{A_3} \right)}$	$GB = \left( \frac{P(1-\Theta)}{2V_{DD}C_L} \right) \cdot \left[ \frac{1}{V_{EB1}} \right]$	$SR = \frac{P(1-\Theta)}{2V_{DD}C_L}$
Folded Cascode $\Theta$ =fraction of current of $M_5$ that is in $M_1$	$A_{V0} = \frac{2\Theta}{V_{EB1}((\Theta\lambda_1 + \lambda_5)\lambda_3V_{EB3} + (1-\Theta)\lambda_9\lambda_7V_{EB9})}$	$GB = \left( \frac{P}{2V_{DD}C_L} \right) \cdot \left[ \frac{\Theta}{V_{EB1}} \right]$	$SR = \frac{\Theta P}{2V_{DD}C_L}$

# Folded Cascode Op Amp (Single-ended Output)



$$A_{v0} \approx \frac{g_{m1}}{(g_{o1} + g_{o5}) \frac{g_{o3}}{g_{m3}} + (g_{o7}) \frac{g_{o9}}{g_{m9}}}$$

$$GB = \frac{g_{m1}}{C_L}$$

How many degrees of freedom are there?

What is a practical design parameter set?

DOF ? **9 DOF**

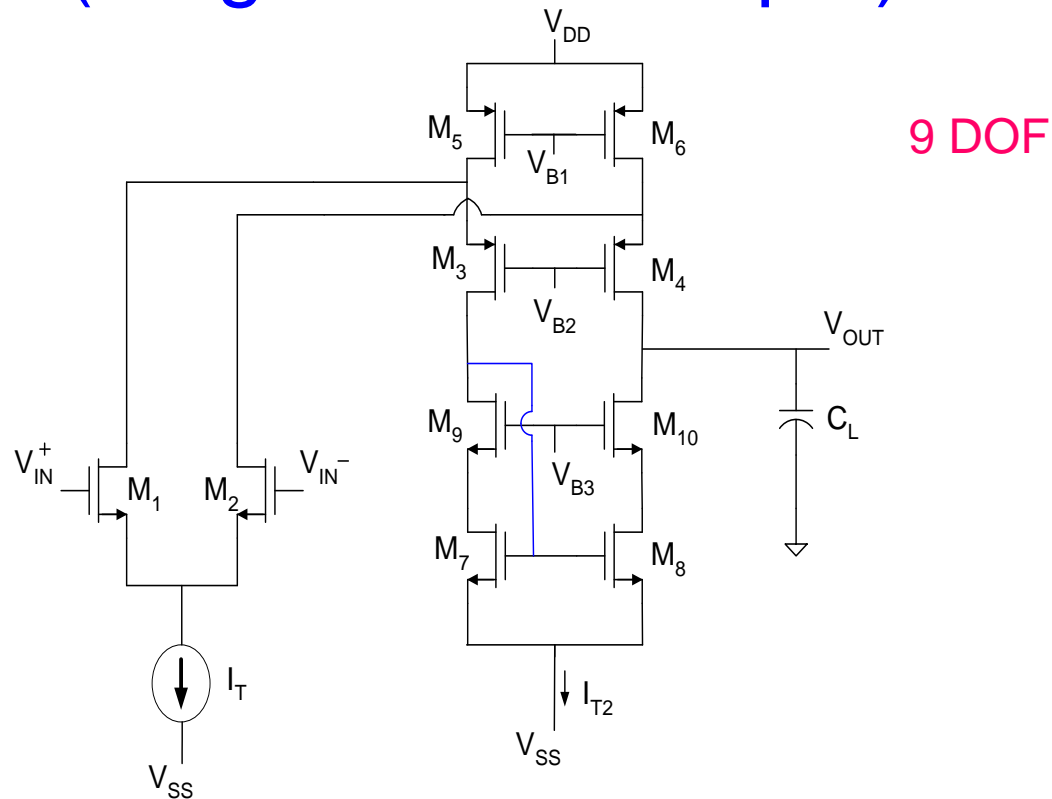
$\{I_T, W_1/L_1, W_5/L_5, W_3/L_3, W_9/L_9, W_7/L_7, V_{B1}, V_{B2}, V_{B3}\}$

Practical Design Parameters

$\{P, \theta, V_{EB1}, V_{EB3}, V_{EB5}, V_{EB7}, V_{EB9}, V_{B2}, V_{B3}\}$

where  $\theta = I_T / (I_T + I_{T2})$

# Folded Cascode Op Amp (Single-ended Output)



Is the 9 DOF an asset or a liability?

Asset

Is this circuit actually used?

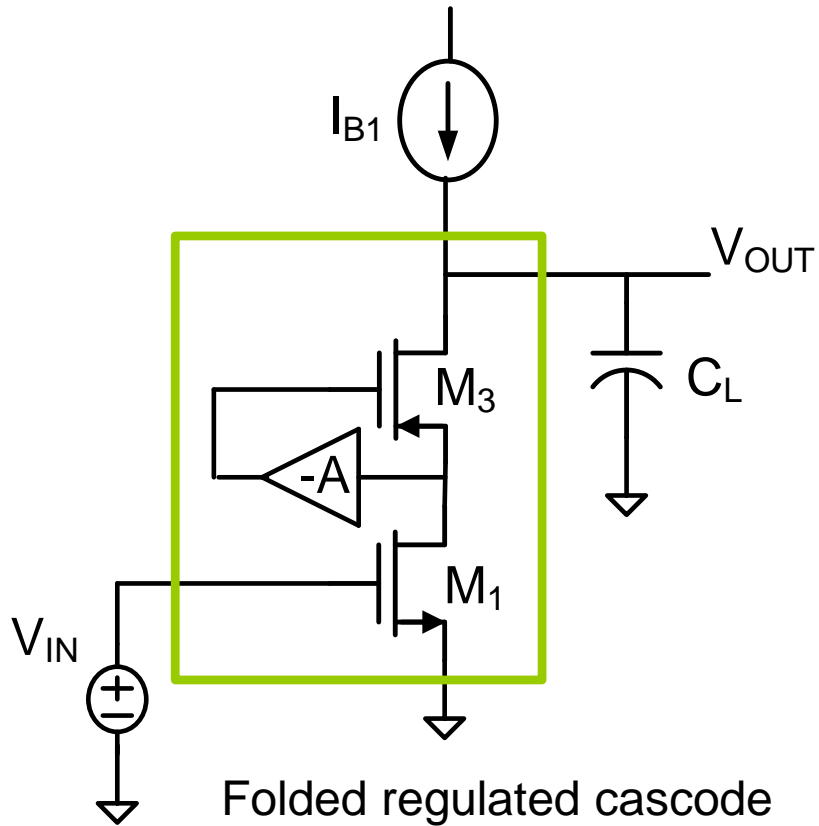
Widely

How many terms would there be in the gain if we did a standard small-signal analysis and did not assume symmetry or differential input?

7 nodal eqns



# What circuit is this?



Can it be used to build a useful op amp?

Textbook reference:

Some of the material we have been discussing appears in Chapter 3, some in Chapter 5, and some in Chapter 6 of the Martin and Johns text

In particular, the telescopic and folded cascode structures are referred to as advanced op amps and appear in later chapters of the text



Stay Safe and Stay Healthy !

**End of Lecture 8**